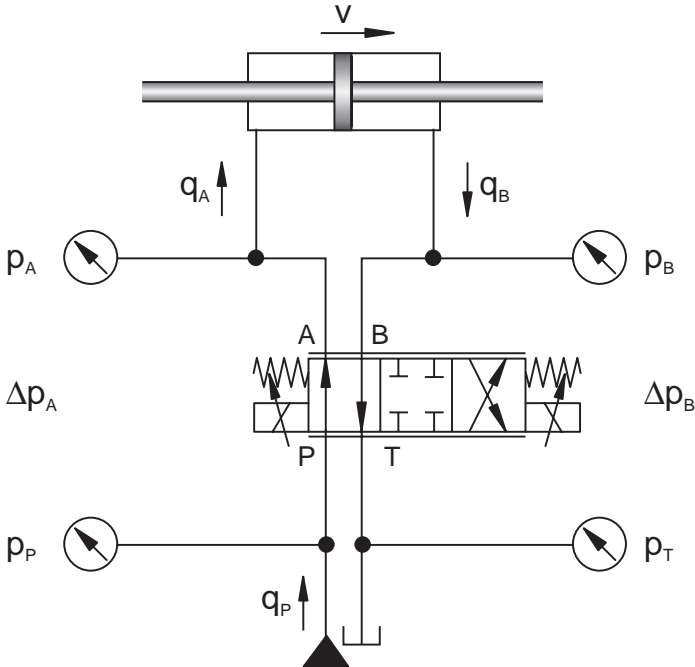


Proportional hydraulics

Textbook



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Chapter 1
Introduction to
proportional hydraulics

Hydraulic drives, thanks to their high power intensity, are low in weight and require a minimum of mounting space. They facilitate fast and accurate control of very high energies and forces. The hydraulic cylinder represents a cost-effective and simply constructed linear drive. The combination of these advantages opens up a wide range of applications for hydraulics in mechanical engineering, vehicle construction and aviation.

The increase in automation makes it ever more necessary for pressure, flow rate and flow direction in hydraulic systems to be controlled by means of an electrical control system. The obvious choice for this are hydraulic proportional valves as an interface between controller and hydraulic system. In order to clearly show the advantages of proportional hydraulics, three hydraulic circuits are to be compared using the example of a feed drive for a lathe (Fig. 1.1):

- a circuit using *manually actuated valves* (Fig. 1.2),
- a circuit using *electrically actuated valves* (Fig. 1.3),
- a circuit using *proportional valves* (Fig. 1.4).

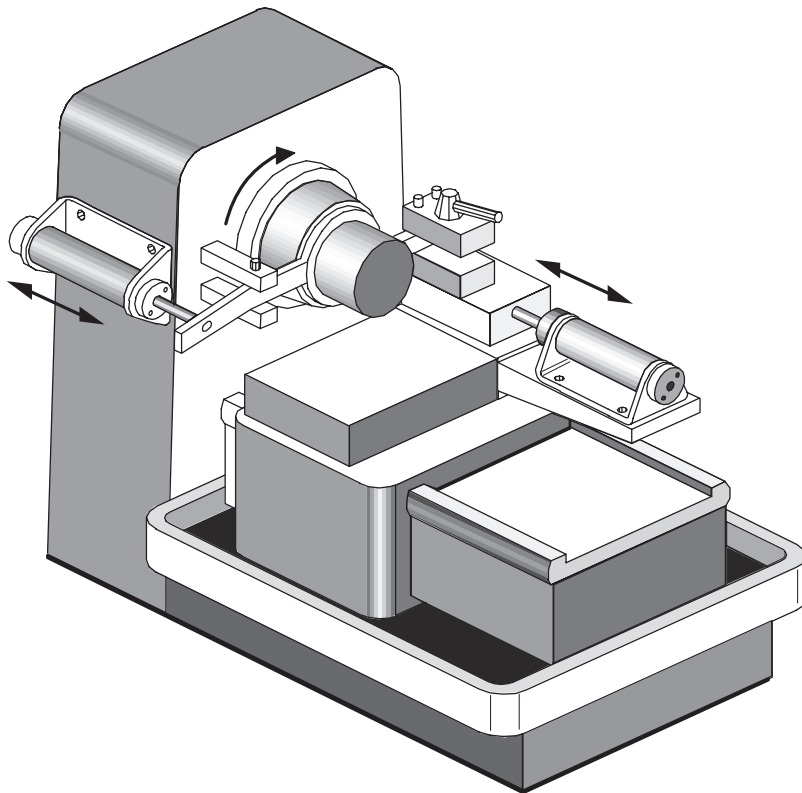


Fig. 1.1
Hydraulic feed
drive of a lathe

1.1 Hydraulic feed drive with manual control

Fig. 1.2 illustrates a circuit using a hydraulic feed drive with manually actuated valves.

- Pressure and flow are to be set during commissioning. To this end, the pressure relief and flow control are to be fitted with setting screws.
- The flow rate and flow direction can be changed during operation by manually actuating the directional control valve.

None of the valves in this system can be controlled electrically. It is not possible to automate the feed drive.

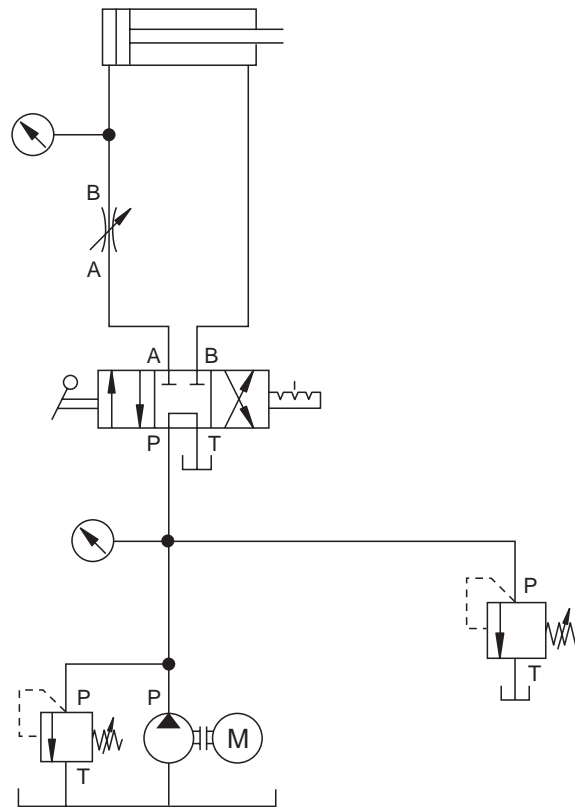


Fig. 1.2
Hydraulic circuit diagram
of a manually controlled
feed drive

In the case of electro-hydraulic systems, the directional control valves are controlled electrically. *Fig 1.3* shows the circuit diagram of a feed drive using an electrically actuated directional control valve. The operation of the lathe can be automated by means of actuating the directional control valve via an electrical control system.

Pressure and flow cannot be influenced during operation by the electrical control system. If a change is required, production on the lathe has to be stopped. Only then can the flow control and pressure relief valve be reset manually.

1.2 Hydraulic feed drive using an electrical control system and switching valves

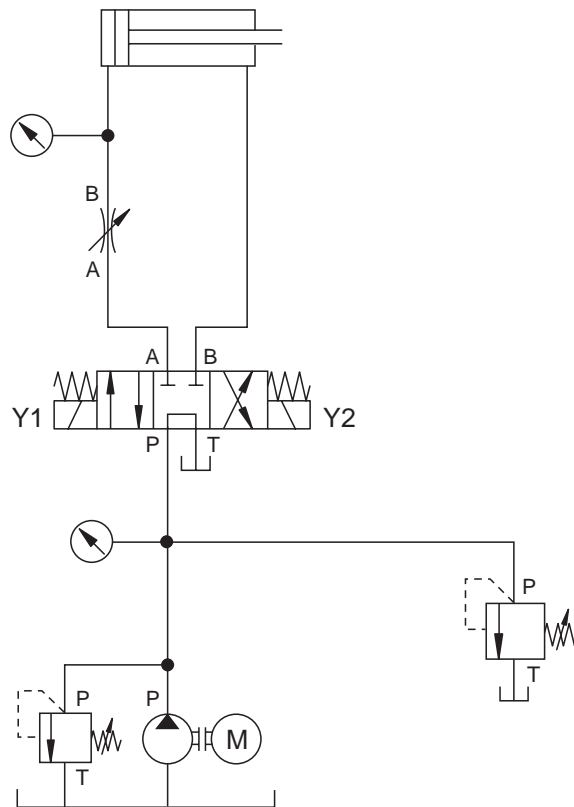


Fig. 1.3
Hydraulic circuit diagram
of an electrically controlled
feed drive

automation of pressure and flow control is only possible to a limited extent with electro-hydraulic control systems using switching valves. Examples are

- the connection of an additional flow control by means of actuating a directional control valve,
- the control of flow and pressure valves with cams.

1.3 Hydraulic feed drive using an electrical control system and proportional valves

In *fig. 1.4*, the hydraulic circuit diagram of a feed drive is shown incorporating proportional valves.

- The proportional directional control valve is actuated by means of an electrical control signal. The control signal influences the flow rate and flow direction. The rate of movement of the drive can be infinitely adjusted by means of changing the flow rate.
- A second control signal acts on the proportional pressure relief valve. The pressure can be continually adjusted by means of this control signal.

The proportional directional control valve in *fig. 1.4* assumes the function of the flow control and the directional control valve in *fig 1.3*. The use of proportional technology saves one valve.

The proportional valves are controlled by means of an electrical control system via an electrical signal, whereby it is possible, during operation,

- to lower the pressure during reduced load phases (e.g. stoppage of slide) via the proportional pressure relief valve and to save energy,
- to gently start-up and decelerate the slide via the proportional directional control valve.

All valve adjustments are effected automatically, i.e. without human intervention.

1.4 Signal flow and components in proportional hydraulics

Fig. 1.5 clearly shows the signal flow in proportional hydraulics.

- An electrical voltage (typically between -10 V and + 10 V) acting upon an electrical amplifier.
- The amplifier converts the voltage (input signal) into a current (output signal).
- The current acts upon the proportional solenoid.
- The proportional solenoid actuates the valve.
- The valve controls the energy flow to the hydraulic drive.
- The drive converts the energy into kinetic energy.

The electrical voltage can be infinitely adjusted and the speed and force (i.e. speed and torque) can be infinitely adjusted on the drive accordingly.

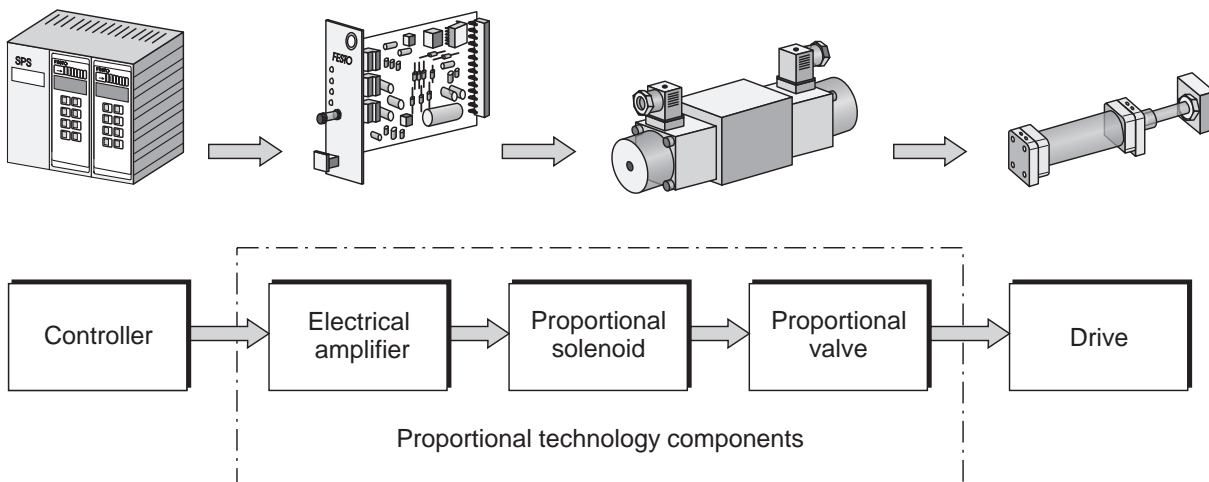


Fig. 1.5:
Signal flow in
proportional hydraulics

Fig. 1.6 illustrates a 4/3-way proportional valve with the appropriate electrical amplifier.

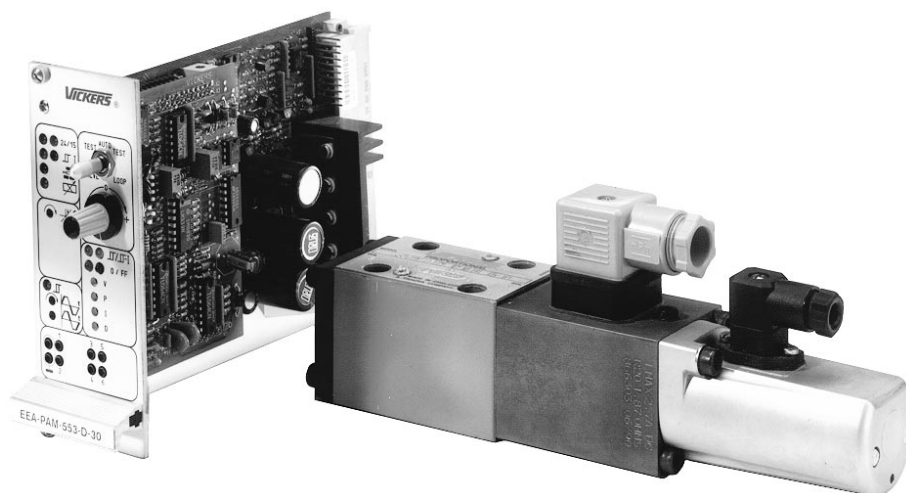


Fig. 1.6
4/3-way proportional
valve with electrical
amplifier (Vickers)

1.5 Advantages of proportional hydraulics **Comparison of switching valves and proportional valves**

The advantages of proportional valves in comparison with switching valves has already been explained in sections 1.2 to 1.4 and are summarised in *table 1.1*.

Adjustability of valves	<ul style="list-style-type: none"> - infinitely adjustable flow and pressure via electrical input signal - automatic adjustment of flow and pressure during operation of system
Effect on the drives	automatable, infinite and accurate adjustment of <ul style="list-style-type: none"> - Force or torque - Acceleration - Velocity or speed - Position or rotary angle
Effect on energy consumption	<ul style="list-style-type: none"> - Energy consumption can be reduced thanks to demand-oriented control of pressure and flow.
Circuit simplification	<ul style="list-style-type: none"> - A proportional valve can replace several valves, e.g. a directional control valve and a flow control valve

*Table 1.1
Advantages of electrically actuated proportional valves compared with switching valves*

Comparison of proportional and servohydraulics

The same functions can be performed with servo valves as those with proportional valves. Thanks to the increased accuracy and speed, servotechnology even has certain advantages. Compared with these, the advantages of proportional hydraulics are the low cost of the system and maintenance requirements:

- The valve design is simpler and more cost-effective.
- The overlap of the control slide and powerful proportional solenoids for the valve actuation increase operational reliability. The need for filtration of the pressure fluid is reduced and the maintenance intervals are longer.
- Servohydraulic drives frequently operate within a closed loop circuit. Drives equipped with proportional valves are usually operated in the form of a control sequence, thereby obviating the need for measuring systems and controller with proportional hydraulics. This correspondingly simplifies system design.

Proportional technology combines the continuous electrical variability and the sturdy, low cost construction of the valves. Proportional valves bridge the gap between switching valves and servo valves.

Chapter 2

Proportional valves: Design and mode of operation

Depending on the design of the valve, either one or two proportional solenoids are used for the actuation of an electrically variable proportional valve.

2.1 Design and mode of operation of a proportional solenoid

Solenoid design

The proportional solenoid (*fig. 2.1*) is derived from the switching solenoid, as used in electro-hydraulics for the actuation of directional control valves. The electrical current passes through the coil of the electro-solenoid and creates a magnetic field. The magnetic field develops a force directed towards the right on to the rotatable armature. This force can be used to actuate a valve.

Similar to the switching solenoid, the armature, barrel magnet and housing of the proportional solenoid are made of easily magnetisable, soft magnetic material. Compared with the switching solenoid, the proportional solenoid has a differently formed control cone, which consists of non-magnetisable material and influences the pattern of the magnetic field lines.

Mode of operation of a proportional solenoid

With the correct design of soft magnetic parts and control cone, the following approximate characteristics (*fig. 2*) are obtained:

- The force increases in proportion to the current, i.e. a doubling of the current results in twice the force on the armature.
- The force does not depend on the position of the armature within the operational zone of the proportional solenoid.

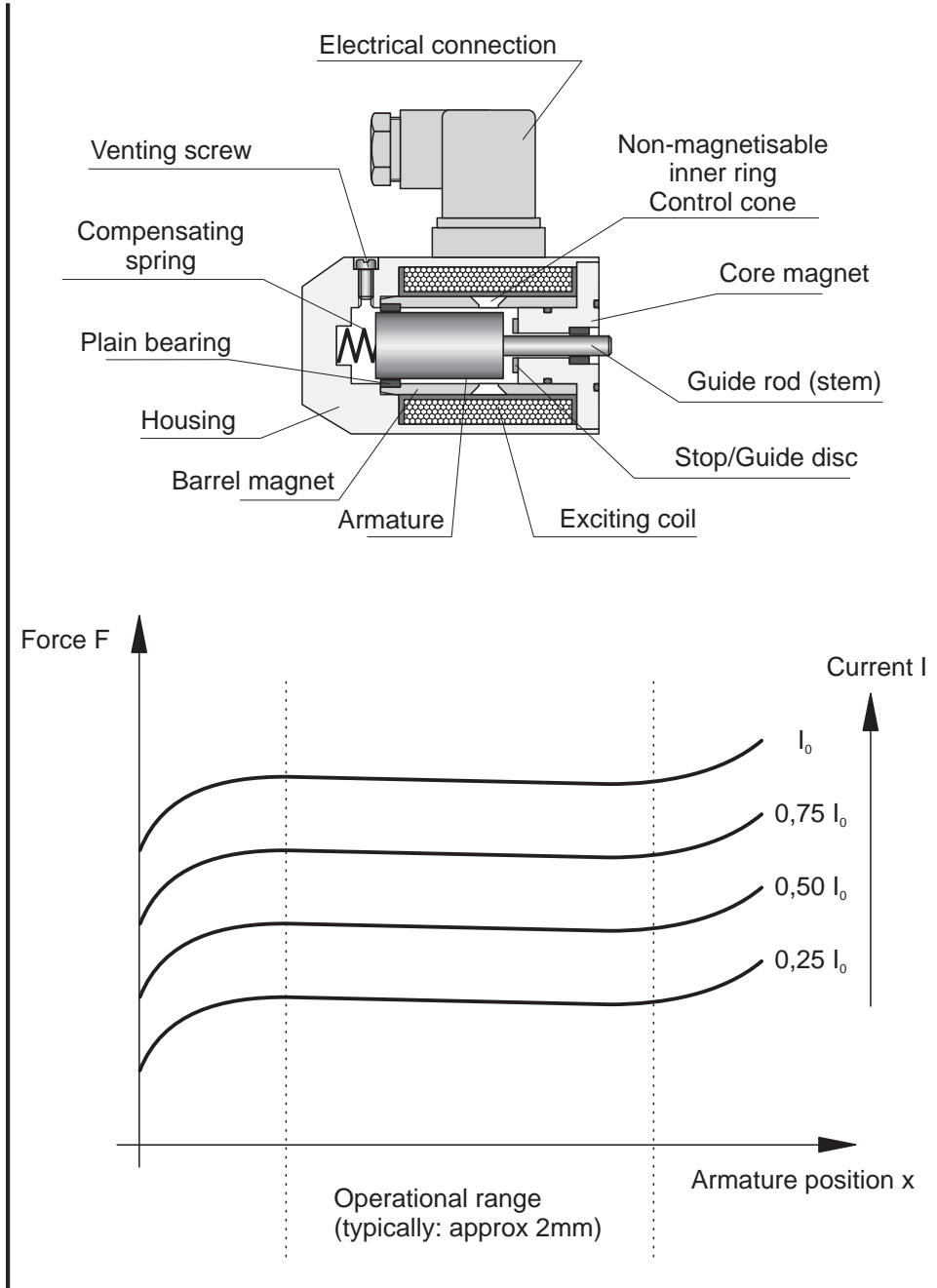


Fig. 2.1
Design and characteristics
of a proportional
solenoid

In a proportional valve, the proportional solenoid acts against a spring, which creates the reset force (fig. 2.2). The spring characteristic has been entered in the two characteristic fields of the proportional solenoid. The further the armature moves to the right, the greater the spring force.

- With a small current, the force on the armature is reduced and accordingly, the spring is almost released. (fig. 2.2a).
- The force applied on the armature increases, if the electrical current is increased. The armature moves to the right and compresses the spring (fig. 2.2b).

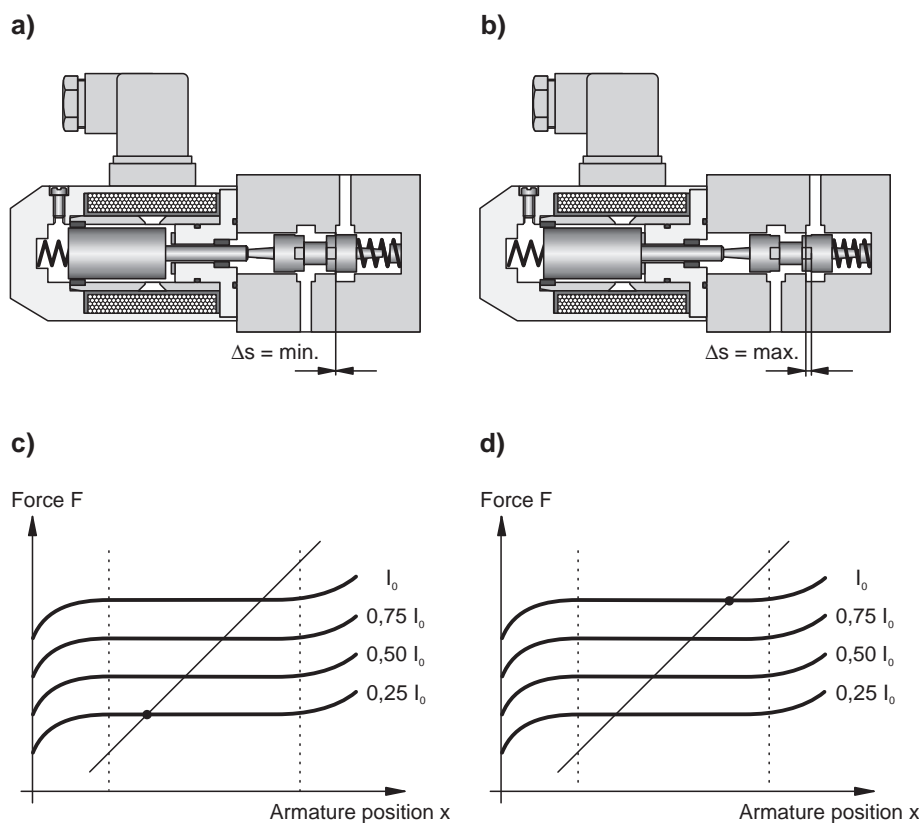


Fig. 2.2
Behaviour of a
proportional solenoid
with different
electrical currents

Actuation of pressure, flow control and directional control valves

In pressure valves, the spring is fitted between the proportional solenoid and the control cone (fig 2.3a).

- With a reduced electrical current, the spring is only slightly pretensioned and the valve readily opens with a low pressure.
- The higher the electrical current set through the proportional solenoid, the greater the force applied on the armature. This moves to the right and the pretensioning of the spring is increased. The pressure, at which the valve opens, increases in proportion to the pretensioning force, i.e. in proportion to the armature position and the electrical current.

In flow control and directional control valves, the control spool is fitted between the proportional solenoid and the spring (fig. 2.3b).

- In the case of reduced electrical current, the spring is only slightly compressed. The spool is fully to the left and the valve is closed.
- With increasing current through the proportional solenoid, the spool is pushed to the right and the valve opening and flow rate increase.

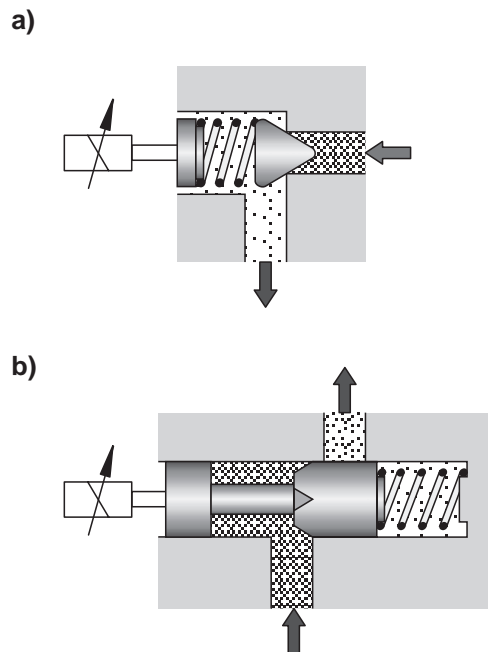


Fig. 2.3
Actuation of a pressure
and a restrictor valve

Positional control of the armature

Magnetising effects, friction and flow forces impair the performance of the proportional valve. This leads to the position of the armature not being exactly proportional to the electrical current.

A considerable improvement in accuracy may be obtained by means of closed-loop control of the armature position (*fig. 2.4*).

- The position of the armature is measured by means of an inductive measuring system.
- The measuring signal x is compared with input signal y .
- The difference between input signal y and measuring signal x is amplified.
- An electrical current I is generated, which acts on the proportional solenoid.
- The proportional solenoid creates a force, which changes the position of the armature in such a way that the difference between input signal y and measuring signal x is reduced.

The proportional solenoid and the positional transducer form a unit, which is flanged onto the valve.

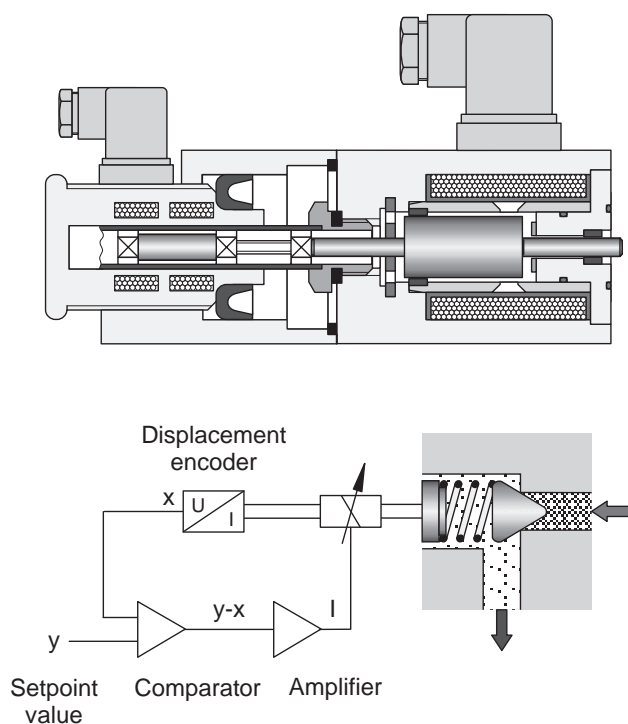


Fig. 2.4
Design of a
position-controlled
proportional solenoid

2.2 Design and mode of operation of proportional pressure valves

With a proportional pressure valve, the pressure in a hydraulic system can be adjusted via an electrical signal.

Pressure relief valve

Fig. 2.5 illustrates a pilot actuated pressure relief valve consisting of a preliminary stage with a poppet valve and a main stage with a control spool. The pressure at port P acts on the pilot control cone via the hole in the control spool. The proportional solenoid exerts the electrically adjustable counterforce.

- The preliminary stage remains closed, if the force of the proportional solenoid is greater than the force produced by the pressure at port P. The spring holds the control spool of the main stage in the lower position; flow is zero.
- If the force exerted by the pressure exceeds the sealing force of the pilot control cone, then this opens. A reduced flow rate takes place to the tank return from port P via port Y. The flow causes a pressure drop via the flow control within the control spool, whereby the pressure on the upper side of the control spool becomes less than the pressure on the lower side. The differential pressure causes a resulting force. The control spool travels upwards until the reset spring compensates this force. The control edge of the main stage opens so that port P and T are connected. The pressure fluid drains to the tank via port T.

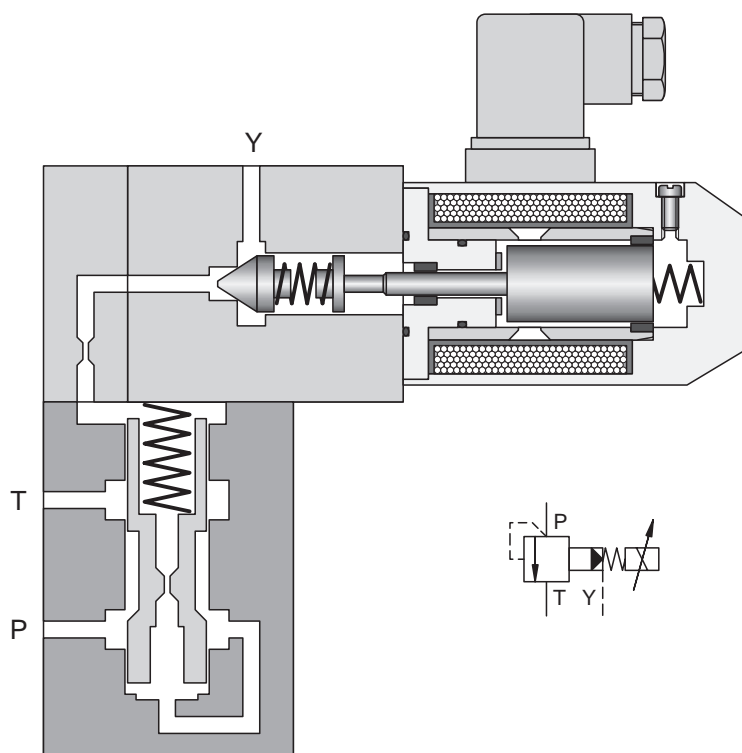


Fig. 2.5
Pilot actuated
proportional pressure
relief valve

Pressure control valve

Fig. 2.6 illustrates a pilot actuated 2-way pressure control valve. The pilot stage is effected in the form of a poppet valve and the main stage as a control spool. The pressure at consuming port A acts on the pilot control cone via the hole in the control spool. The counter force is set via the proportional solenoid.

- If the pressure at port A is below the preset value, the pilot control remains closed. The pressure on both sides of the control spool is identical. The spring presses the control spool downwards and the control edge of the main stage is open. The pressure fluid is able to pass unrestricted from port P to port A.
- If pressure at port A exceeds the preset value, the pilot stage opens so that a reduced flow passes to port Y. The pressure drops via the flow control in the control spool. The force on the upper side of the control spool drops and the control spool moves upwards. The cross section of the opening is reduced. As a result of this, the flow resistance of the control edge between port P and port A increases. Pressure at port A drops.

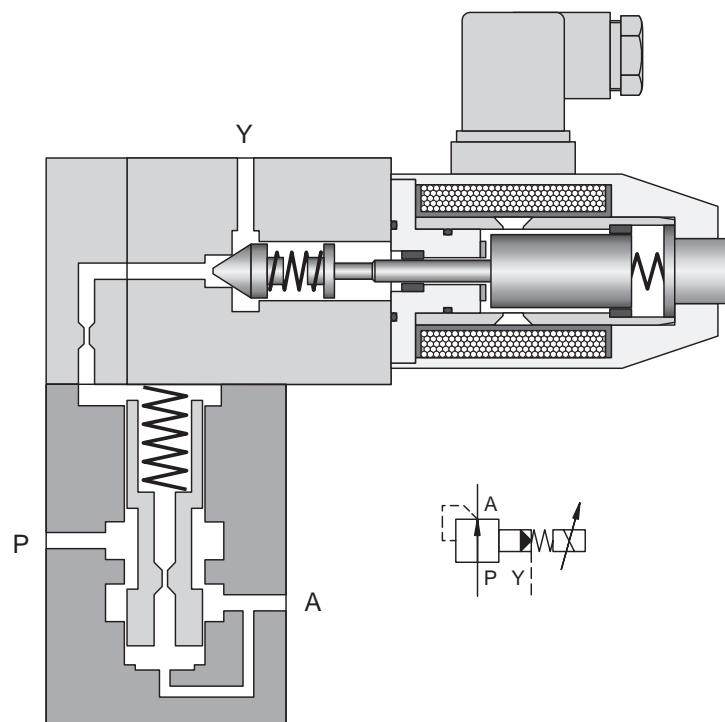


Fig. 2.6
Pilot actuated
proportional
pressure control valve

Proportional flow control valve

In the case of a proportional flow control valve in a hydraulic system, the throttle cross section is electrically adjusted in order to change the flow rate.

A proportional flow control valve is similarly constructed to a switching 2/2-way valve or a switching 4/2-way valve.

With a directly actuated proportional flow control valve (fig. 2.7), the proportional solenoid acts directly on the control spool.

- With reduced current through the proportional solenoid, both control edges are closed.
- The higher the electrical current through the proportional solenoid, the greater the force on the spool. The spool moves to the right and opens the control edges.

The current through the solenoid and the deflection of the spool are proportional.

2.3 Design and mode of operation of proportional flow control and directional control valves

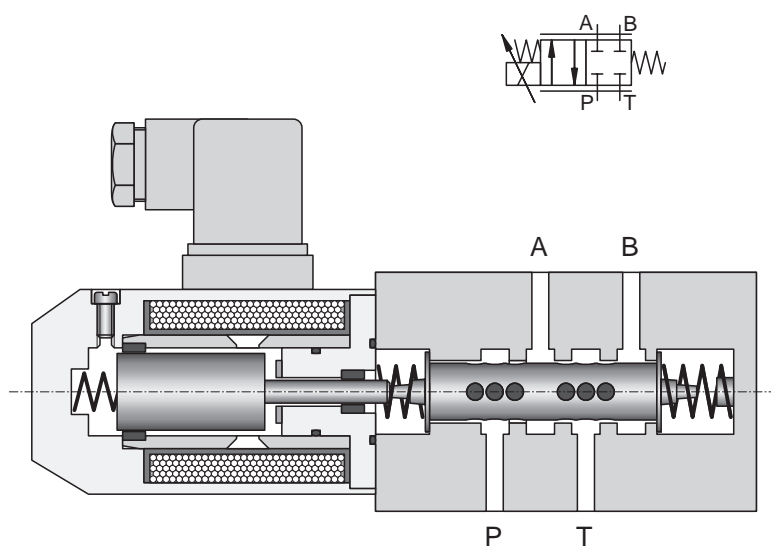


Fig. 2.7
Directly actuated proportional restrictor valve without position control

Directly actuated proportional directional control valve

A proportional directional control valve resembles a switching 4/3-way valve in design and combines two functions:

- Electrically adjustable flow control (same as a proportional flow control valve),
- Connection of each consuming port either with P or with T (same as a switching 4/3-way valve).

Fig 2.8 illustrates a directly actuated proportional directional control valve.

- If the electrical signal equals zero, then both solenoids are de-energised. The spool is centred via the springs. All control edges are closed.
- If the valve is actuated via a negative voltage, the current flows through the righthand solenoid. The spool travels to the left. Ports P and B as well as A and T are connected together. The current through the solenoid and the deflection of the spool are proportional.
- With a positive voltage, the current flows through the lefthand solenoid. The spool moves to the right. Ports P and A as well as B and T are connected together. In this operational status too, the electrical current and the deflection of the spool are proportional to one another.

In the event of power failure, the spool moves to the mid-position so that all control edges are closed. (fail-safe position).

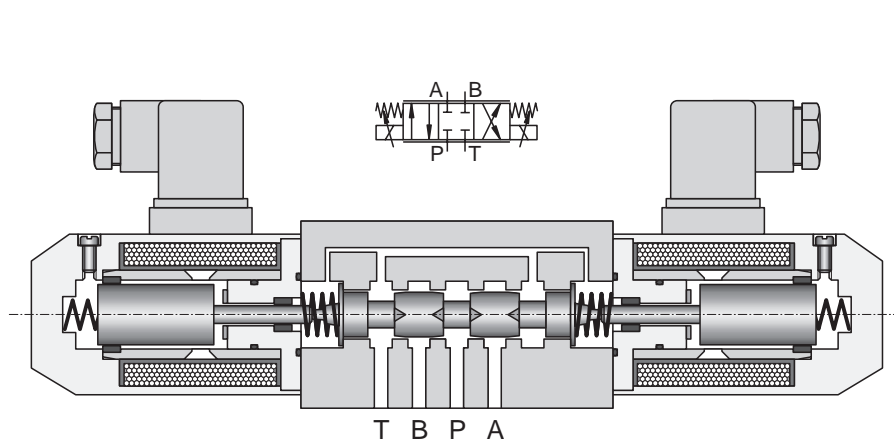


Fig. 2.8
Directly actuated
proportional directional control valve without
position control

Pilot actuated proportional directional control valve

Fig. 2.9 shows a pilot actuated proportional directional control valve. A 4/3-way proportional valve is used for pilot control. This valve is used to vary the pressure on the front surfaces of the control spool, whereby the control spool of the main stage is deflected and the control edges opened. Both stages in the valve shown here are position controlled in order to obtain greater accuracy.

In the event of power or hydraulic energy failure, the control spool of the main stage moves to the mid-position and all control edges are closed (fail-safe position).

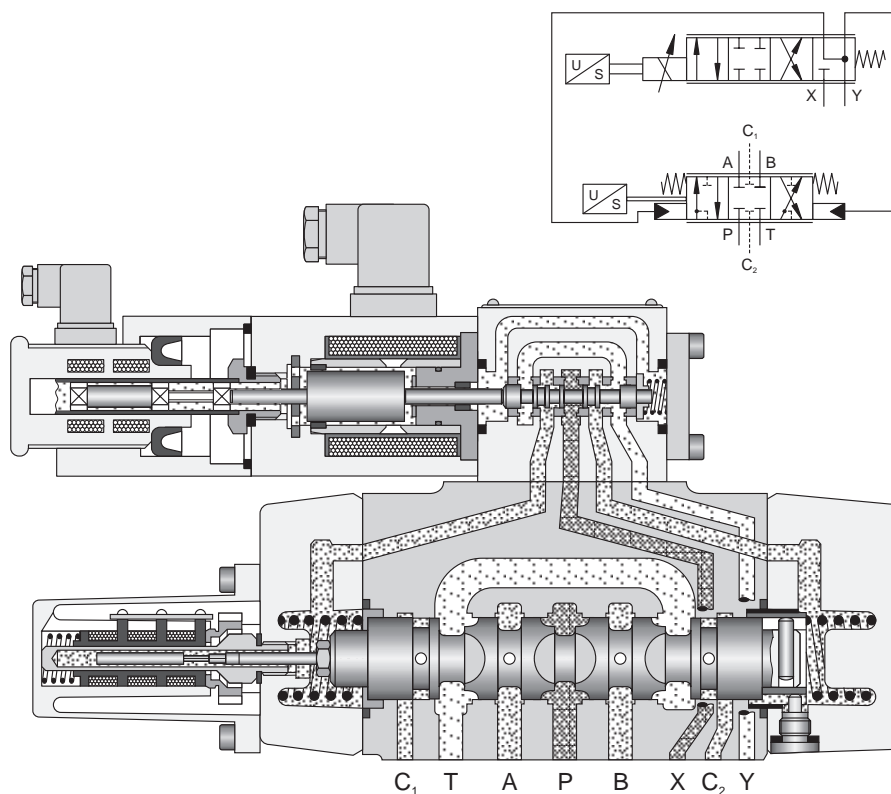


Fig. 2.9
Pilot actuated
proportional directional control
valve

Two 3-way pressure regulators may be used for pilot control instead of a 4/3-way valve. Each pressure valve controls the pressure on one front surface of the main stage control spool.

Advantages and disadvantages of pilot actuated proportional valves

The force for the actuation of the main stage is generated hydraulically in the pilot actuated valve. Only the minimal actuating force for the initial stage has to be generated by the proportional solenoid. The advantage of this is that a high level of hydraulic power can be controlled with a small proportional solenoid and a minimum of electrical current. The disadvantage is the additional oil and power consumption of the pilot control.

Proportional directional control valves up to nominal width 10 are primarily designed for direction actuation. In the case of valves with greater nominal width, the preferred design is pilot control. Valves with very large nominal width for exceptional flow rates may have three or four stages.

2.4 Design and mode of operation of proportional flow control valves

With proportional flow control and directional control valves, the flow rate depends on two influencing factors:

- the opening of the control edge specified via the control signal,
- the pressure drop via the valve.

To ensure that the flow is only affected by the control signal, the pressure drop via the control edge must be maintained constant. This is achieved by means of an additional pressure balance and can be realised in a variety of ways:

- Pressure balance and control edge are combined in one flow control valve.
- The two components are combined by means of connection technology.

Fig. 2.10 shows a section through a 3-way proportional flow control valve. The proportional solenoid acts on the lefthand spool. The higher the electrical current through the proportional solenoid is set, the more control edge A-T opens and the greater the flow rate.

The righthand spool is designed as a pressure balance. The pressure at port A acts on the lefthand side of the spool and the spring force and the pressure at port T on the righthand side.

- If the flow rate through the valve is too great, the pressure drop on the control edge rises, i.e. the differential pressure A-T. The control spool of the pressure balance moves to the right and reduces the flow rate at control edge T-B. This results in the desired reduction of flow between A and B.
- If the flow rate is too low, the pressure drop at the control edge falls and the control spool of the pressure balance moves to the left. The flow rate at control edge T-B rises and the flow increases.

In this way, flow A-B is independent of pressure fluctuations at both ports.

If port P is closed, the valve operates as a 2-way flow control valve. If port P is connected to the tank, the valve operates as a 3-way flow control valve.

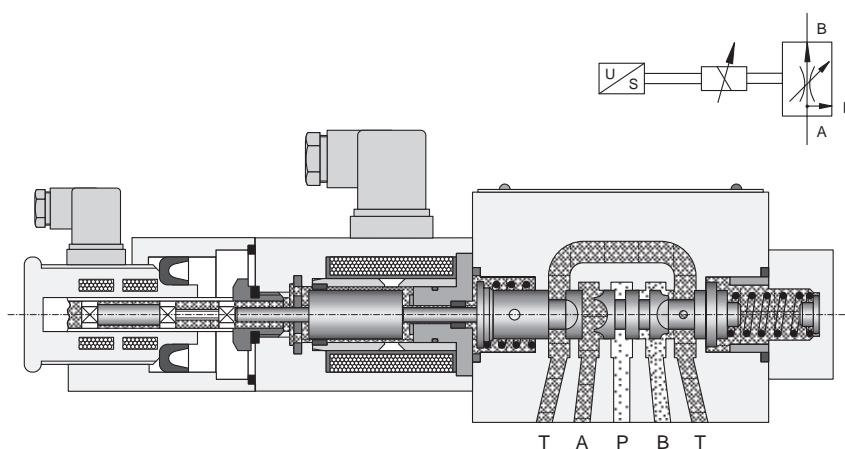


Fig. 2.10
Proportional
flow control valve

2.5 Proportional valve designs: overview

Proportional valves differ with regard to the type of valve, the control and the design of the proportional solenoid (table 2.1). Each combination from table 2.1 results in one valve design, e.g.

- a directly actuated 2/2-way proportional flow control valve without positional control,
- a pilot actuated 4/3-way proportional valve with positional control,
- a directly actuated 2-way proportional flow control valve with positional control.

Valve types	- Pressure valves	Pressure relief valve 2-way pressure regulator 3-way pressure regulator
	- Restrictor valves	4/2-way restrictor 2/2-way restrictor valve
	- Directional control valves	4/3-way valve 3/3-way valve
	- Flow control valves	2-way flow control valve 3-way flow control valve
Control type	- directly actuated - pilot actuated	
Proportional solenoid	- without position control - position controlled	

Table 2.1
Criteria for proportional valves

Chapter 3

Proportional valves: Characteristic curves and parameters

Table 3.1 provides an overview of proportional valves and variables in a hydraulic system controlled by means of proportional valves.

3.1 Characteristic curve representation

Valve types	Input variable	Output variable
Pressure valve	electr. current	Pressure
Restrictor valve	electr. current	Valve opening, Flow (pressure-dependent)
Directional control valve	electr. current	Valve opening Flow direction Flow (pressure dependent)
Flow control valve	electr. current	Flow (pressure independent)

Table 3.1
Proportional valves:
Input and
output variables

The correlation between the input signal (electrical current) and the output signal (pressure, opening, flow direction or flow rate) can be represented in graphic form, whereby the signals are entered in a diagram:

- the input signal in X-direction,
- the output signal in Y-direction.

In the case of proportional behaviour, the characteristic curve is linear (fig. 3.1). The characteristic curves of ordinary valves deviate from this behaviour.

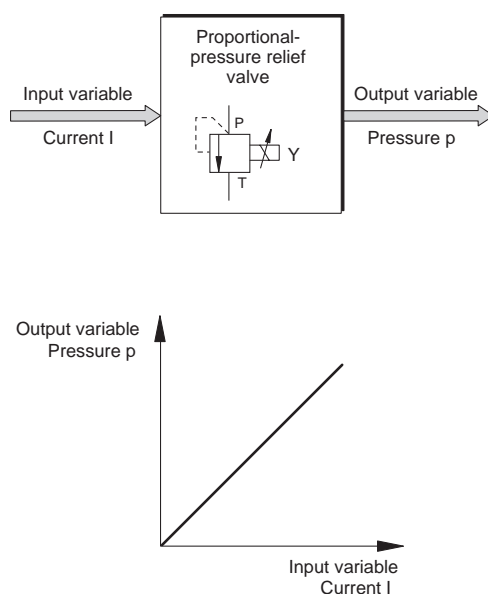


Fig. 3.1
Characteristic of a
proportional pressure
relief valve

3.2 Hysteresis, inversion range and response threshold

Deviations from ideal behaviour occur as a result of spool friction and the magnetising effects, such as:

- the response threshold,
- the inversion range,
- the hysteresis.

Response threshold

If the electrical current through the proportional solenoid is increased, the armature of the proportional solenoid moves. As soon as the current ceases to change (*fig. 3.2a*), the armature remains stationary. The current must then be increased by a minimum amount, before the armature moves again. The required minimum variation is known as the response threshold or response sensitivity, which also occurs if the current is reduced and the armature moves in the other direction.

Inversion range

If the input signal is first changed in the positive and then in the negative direction, this results in two separate branch characteristics, see diagram (*fig. 3.2b*). The distance of the two branches is known as the inversion range. The same inversion range results, if the current is first of all changed in the negative and then in the positive direction.

Hysteresis

If the current is changed to and fro across the entire correcting range, this results in the maximum distance between the branch characteristics. The largest distance between the two branches is known as hysteresis (*fig. 3.2c*).

The values of the response threshold, inversion range and hysteresis are reduced by means of positional control. Typical values for these three variables are around

- 3 to 6% of the correcting range for unregulated valves
- 0.2 to 1% of the correcting range for position controlled valves

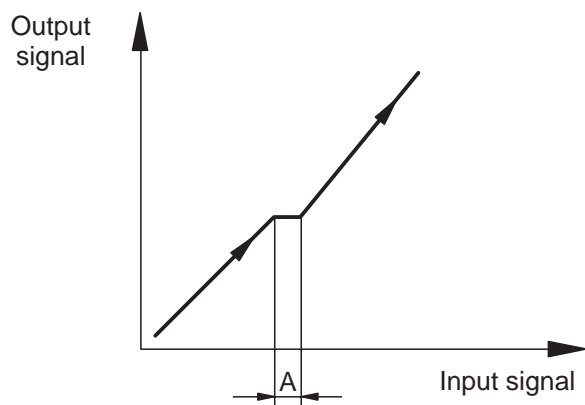
Sample calculation for a flow control valve without positional control:

Hysteresis: 5% of correcting range,

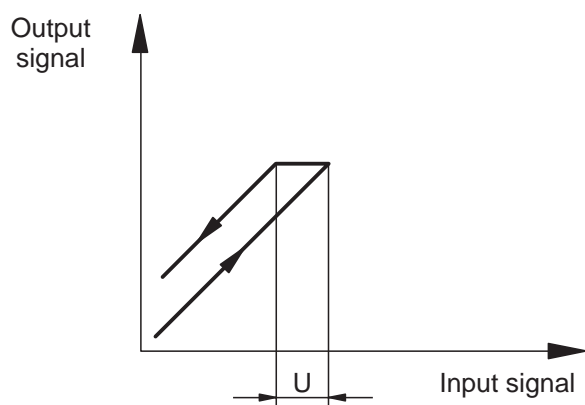
Correcting range: 0...10 V

Distance of branch characteristics = $(10 \text{ V} - 0 \text{ V}) 5\% = 0.5 \text{ V}$

a) Response threshold



b) Inversion range



c) Hysteresis

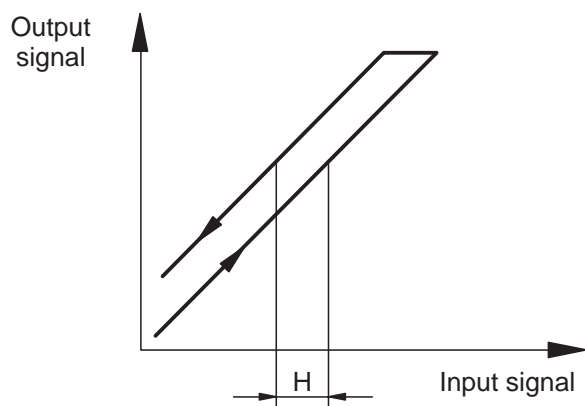


Fig. 3.2
Response threshold,
inversion range and
hysteresis

3.3 Characteristic curves of pressure valves

The behaviour of the pressure valves is described by the pressure/signal function. The following are plotted:

- the electrical current in X-direction
- the pressure at the output of the valve in Y-direction.

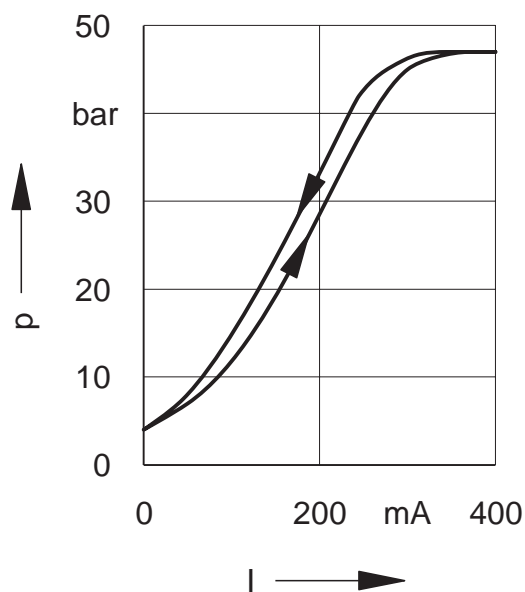


Fig. 3.3
Pressure/signal function
of a pilot actuated
pressure relief valve

3.4 Characteristic curves of flow control and directional control valves

With flow control and directional control valves the deflection of the spool is proportional to the electrical current through the solenoid (fig. 2.7).

Flow/signal function

A measuring circuit to determine the flow/signal function is shown in fig. 3.4. When recording measurements, the pressure drop above the valve is maintained constant. The following are plotted

- the current actuating the proportional solenoid in X-direction,
- the flow through the valve in Y-direction.

The flow rises not only with an increase in current through the solenoid, but also with an increase in pressure drop above the valve. This is why the differential pressure at which the measurement has been conducted is specified in the data sheets. Typical is a pressure drop of 5 bar, 8 bar or 35 bar per control edge.

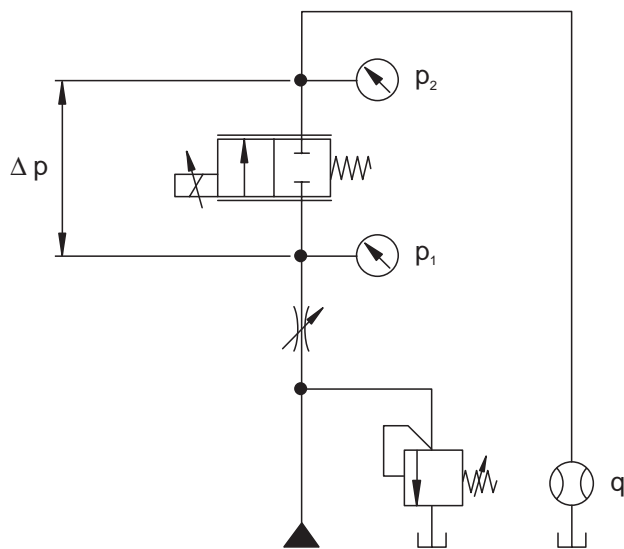


Fig. 3.4
Measurement of flow/
signal function

Additional variables influencing the flow/signal function are

- the overlap,
- the shape of the control edges.

Overlap

The overlap of the control edges influences the flow/signal function. Fig. 3.5 clarifies the correlation between overlap and flow/signal function using the examples of a proportional directional control valve:

- In the case of positive overlap, a reduced electrical current causes a deflection of the control spool, but the flow rate remains zero. This results in a dead zone in the flow/signal function.
- In the case of zero overlap, the flow/signal function in the low-level signal range is linear.
- In the case of negative overlap, the flow/signal function in the small valve opening range results in a greater shape.

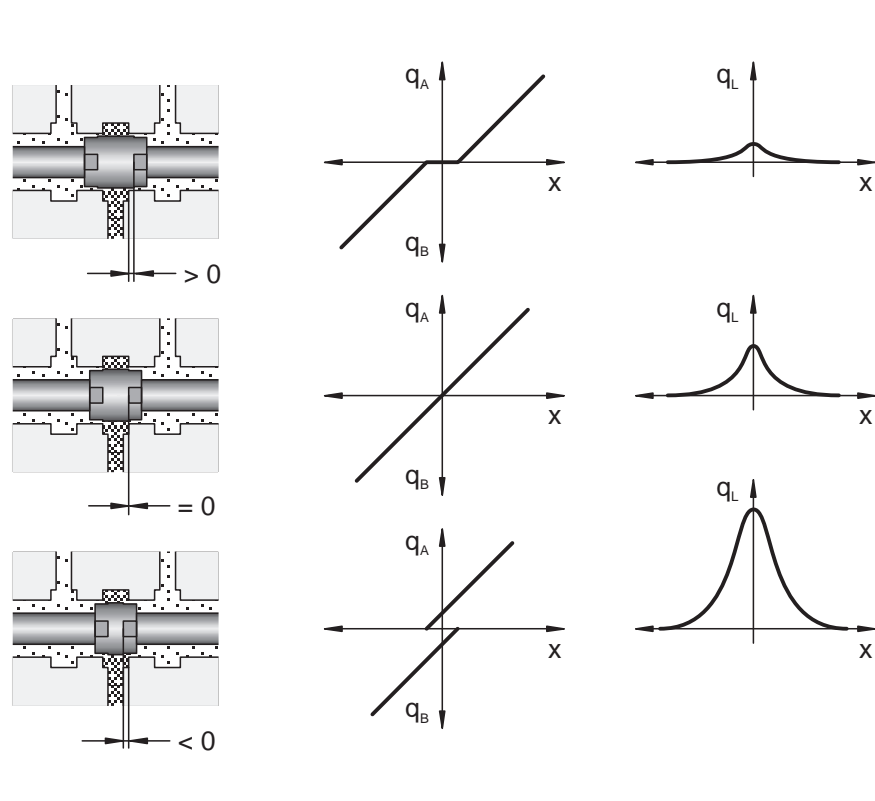


Fig. 3.5
Overlap and
Flow/signal function

In practice, proportional valves generally have a positive overlap. This is useful for the following reasons:

- The leakage in the valve is considerably less in the case of a spool mid-position than with a zero or negative overlap.
- In the event of power failure, the control spool is moved into mid-position by the spring force (fail-safe position). Only with positive overlap does the valve meet the requirement of closing the consuming ports in this position.
- The requirements for the finishing accuracy of a control spools and housing are less stringent than that for zero overlap.

Control edge dimensions

The control edges of the valve spool can be of different form. The following vary (*fig. 3.6*):

- shapes of control edges,
- the number of openings on the periphery,
- the spool body (solid or drilled sleeve).

The drilled sleeve is the easiest and most cost effective to produce.

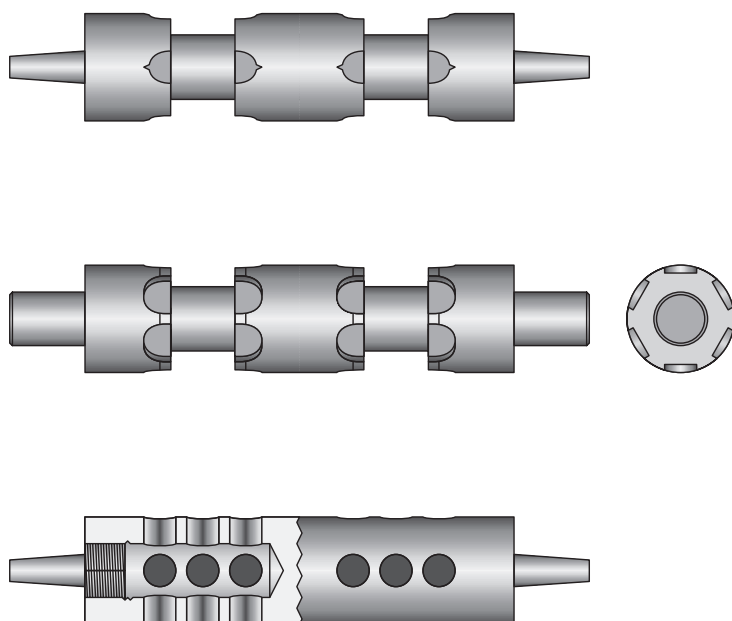


Fig. 3.6
Spool with different
control edge patterns

Very frequently used is the triangular shaped control edge. Its advantages can be clarified on a manually operated directional control valve:

- With a closed valve, leakage is minimal due to the overlap and the triangular shaped openings.
- Within the range of small openings, lever movements merely produce slight flow variations. Flow rate in this range can be controlled with a very high degree of sensitivity.
- Within the range of large openings, large flow variations are achieved with small lever deflections.
- If the lever is moved up to the stop, a large valve opening is obtained; consequently a connected hydraulic drive reaches a high velocity.

Similar to the hand lever, a proportional solenoid also permits continuous valve adjustment. All the advantages of the triangular type control edges therefore also apply for the electrically actuated proportional valve.

Fig. 3.7
Manually operated valve
with triangular
control edge

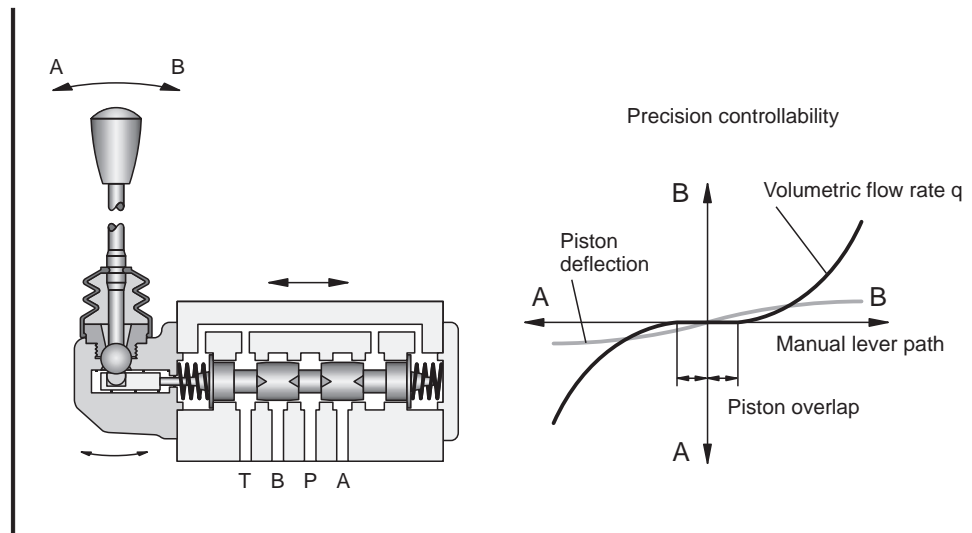


Fig. 3.8 illustrates the flow/signal function for two different types of control edge:

- With reduced electrical current, both control edges remain closed due to the positive overlap.
- The rectangular control edge causes a practically linear pattern of the characteristic curve.
- The triangular control edge results in a parabolic flow/signal function.

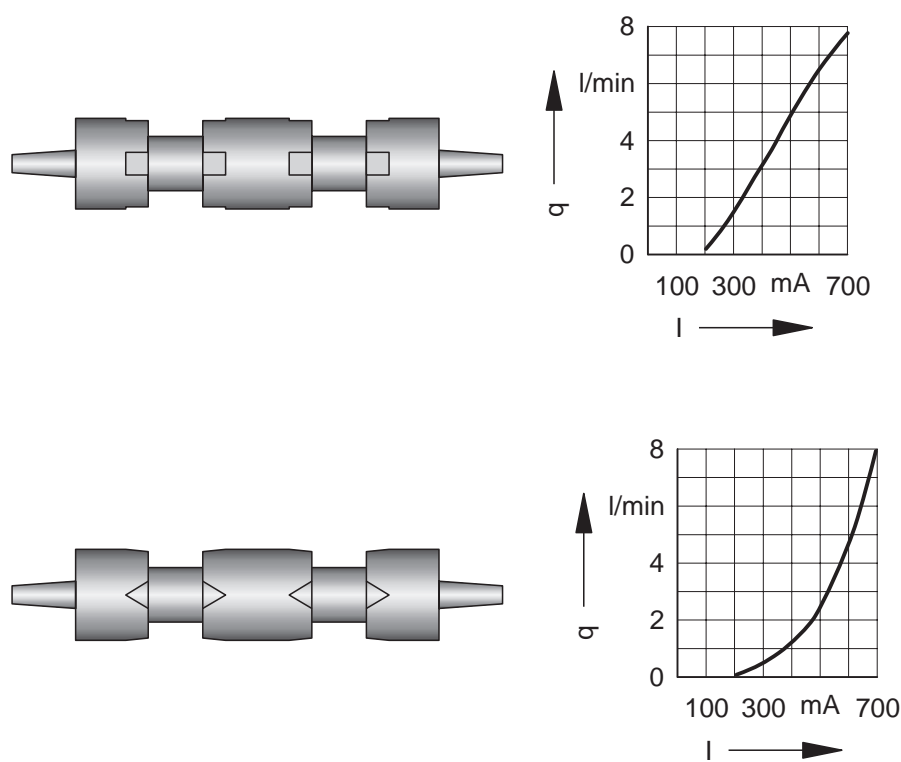


Fig. 3.8
Flow/signal functions for
two different spool patterns

3.5 Parameters of valve dynamics

Many applications require proportional valves, which are not only able to follow the changes of the electrical input accurately, but also very quickly. The speed of reaction of a proportional valve can be specified by means of two characteristic values:

1. **Manipulating time:**

designates the time required by the valve to react to a change in the correcting variable. Fast valves have a small manipulating time.

2. **Critical frequency:**

indicates how many signal changes per second the valve is able to follow. Fast valves demonstrate a high critical frequency.

Manipulating time

The manipulating time of a proportional valve is determined as follows:

- The control signal is changed by means of a step change.
- The time required by the valve to reach the new output variable is measured.

The manipulating time increases with large signal changes (*fig. 3.9*). Moreover, a large number of valves have a different manipulating time for positive and negative control signal changes.

The manipulating times of proportional valves are between approx. 10 ms (fast valve, small control signal change) and approx. 100 ms (slow valve, large control signal change).

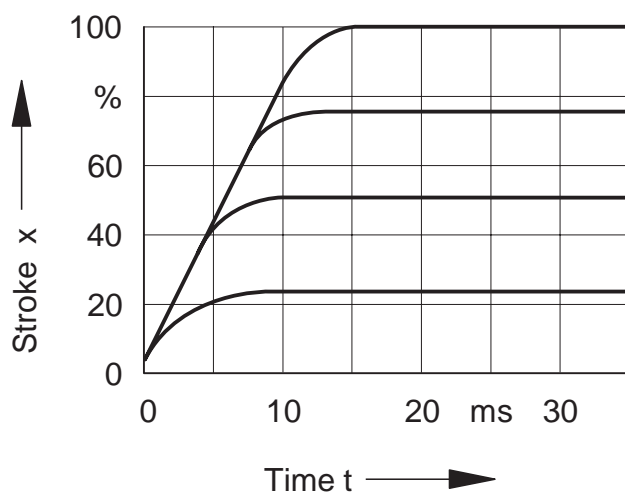


Fig. 3.9
Manipulating time
for different control
signal jumps
(Proportional directional
control valve)

Frequency response measurement

In order to be able to specify the critical frequency of a valve, it is first necessary to measure the frequency response.

To measure the frequency response, the valve is actuated via a sinusoidal control signal. The correcting variable and the spool position are represented graphically by means of an oscilloscope. The valve spool oscillates with the same frequency as the control signal (*fig. 3.10*).

If the actuating frequency is increased whilst the activating amplitude remains the same, then the frequency with which the spool oscillates also increases. With very high frequencies, the spool is no longer able to follow the control signal changes. The amplitude A_2 in *fig. 3.10e* is clearly smaller than the amplitude A_1 in *fig. 3.10d*.

a) Measuring circuit

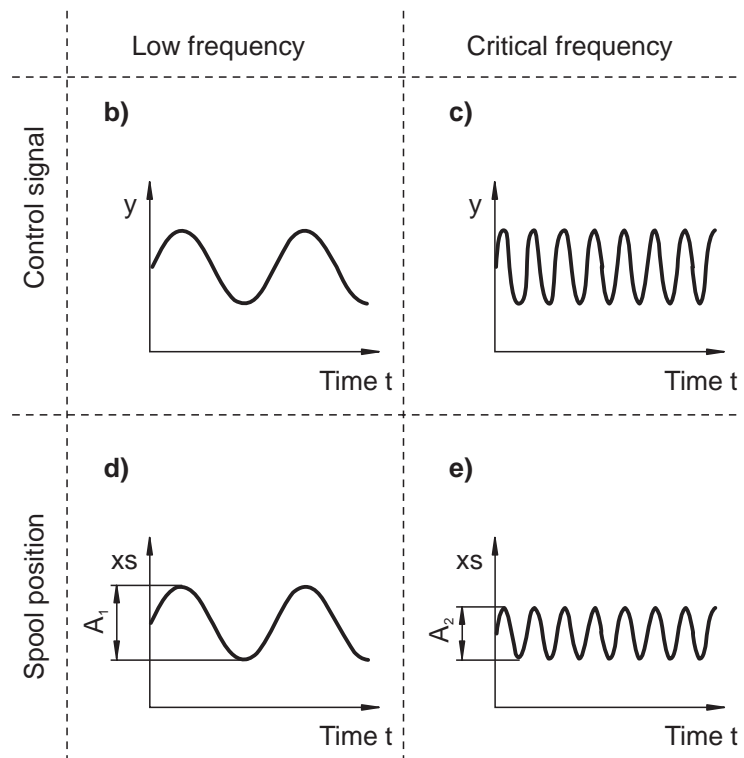
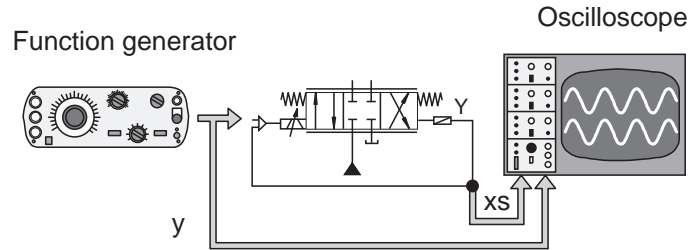


Fig. 3.10:
Measurement of frequency
response with a
proportional directional
control valve

The frequency response of a valve consists of two diagrams:

- the amplitude response,
- the phase response.

Amplitude response

The ratio of the amplitude at measured frequencies to the amplitude at very low frequencies is specified in dB and plotted in logarithmic scale. An amplitude ratio of -20 dB means that the amplitude has dropped to a tenth of the amplitude at low frequency. If the amplitude for all measured values is plotted against the measured frequency, this produces the amplitude response (*fig. 3.11*).

Phase response

The delay of the output signal with regard to the input signal is specified in degrees. A 360 degree phase displacement means that the output signal lags behind the input signal by an entire cycle. If all the phase values are plotted against the measuring frequency, this results in the phase response (*fig. 3.11*).

Frequency response and control signal amplitude

With a 10% correcting variable amplitude (= 1 volt), the control spool only needs to cover a small distance. Consequently, the control spool is also able to follow signal changes with a high frequency. Amplitude and phase response only inflect with a high frequency from the horizontal (*fig. 3.11*).

With a 90% correcting variable amplitude (= 9 Volt), the required distance is nine times as great. Accordingly, it is more difficult for the control spool to follow the control signal changes. Amplitudes and phase response already inflect at a low frequency from the horizontal (*fig. 3.11*).

Critical frequency

The critical frequency is read from the amplitude response. It is the frequency, at which the amplitude response has dropped to 70.7% or -3 dB.

The frequency response (*fig. 3.11*) results in a critical frequency of approx. 65 Hertz at 10% of the maximum possible control signal amplitude. For 90% control signal amplitude the critical frequency is at approx. 23 Hertz.

The critical frequencies of proportional valves are between approx. 5 Hertz (slow valve, large control signal amplitude) and approx. 100 Hertz (fast valve, small control signal amplitude).

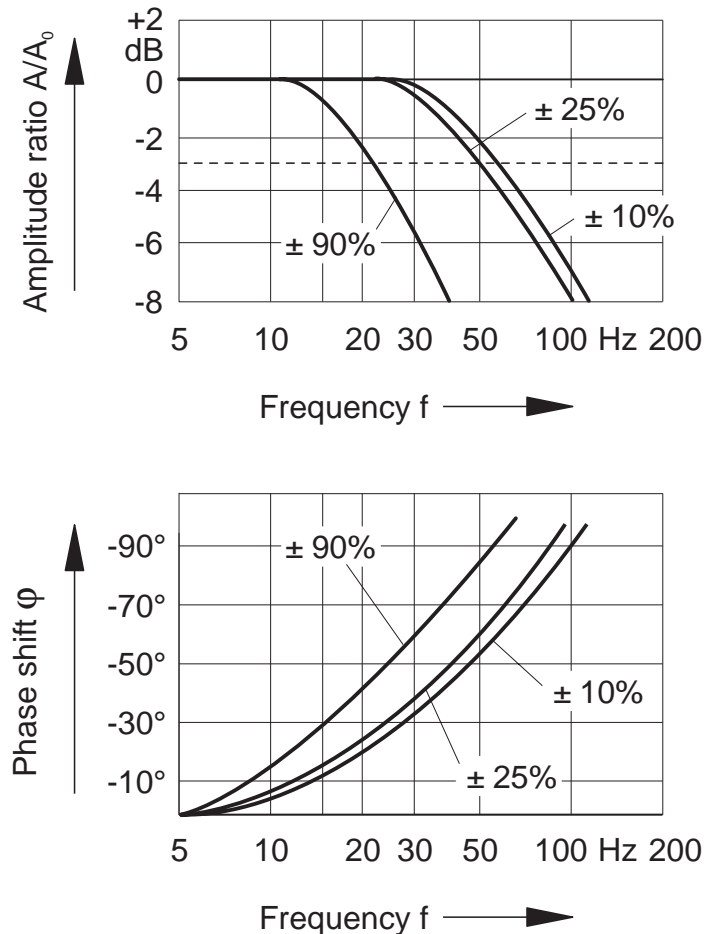


Fig. 3.11
Frequency response of a
proportional directional
control valve

3.6 Application limits of proportional valves

The application limits of a proportional valve are determined by

- the pressure strength of the valve housing,
- the maximum permissible flow force applied to the valve spool.

If the flow force becomes too great, the force of the proportional solenoid is not sufficient to hold the valve spool in the required position. As a result of this, the valve assumes an undefined status.

The application limits are specified by the manufacturer either in the form of numerical values for pressure and flow rate or in the form of a diagram.

Chapter 4

Amplifier and setpoint value specification

The control signal for a proportional valve is generated via an electronic circuit. *Fig. 4.1* illustrates the signal flow between the control and proportional solenoid. Differentiation can be made between two functions:

- **Setpoint value specification:**
The correcting variable (= setpoint value) is generated electronically. The control signal is output in the form of an electrical voltage. Since only a minimal current flows, the proportional solenoid cannot be directly actuated.
- **Amplifier:**
The electrical amplifier converts the electrical voltage in the form of an input signal into a electrical current in the form of an output signal. It provides the electrical power required for the valve actuation.

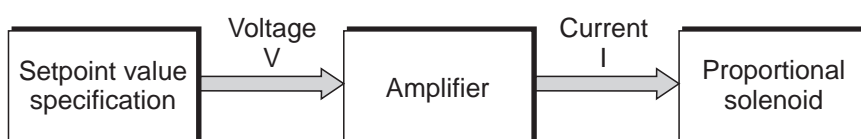


Fig. 4.1
Signal flow between controller and proportional solenoid (schematic)

Modules

The setpoint value specification and amplifier can be grouped into electronic modules (electronic cards) in various forms. Three examples are illustrated in *fig. 4.2*.

- A control system, which can only process binary signals is used (e.g. simple PLCs). Setpoint value specification and amplifier constitute separate modules (*fig. 4.2a*).
- A PLC with analogue outputs is used. The correcting variable is directly generated, including special functions such as ramp generation and quadrant recognition. No separate electronics are required for the setpoint value specification (*fig. 4.2b*).
- Mixed forms are frequently used. If the control is only able to specify constant voltage values, additional functions such as ramp generation are integrated in the amplifier module (*fig. 4.2c*).

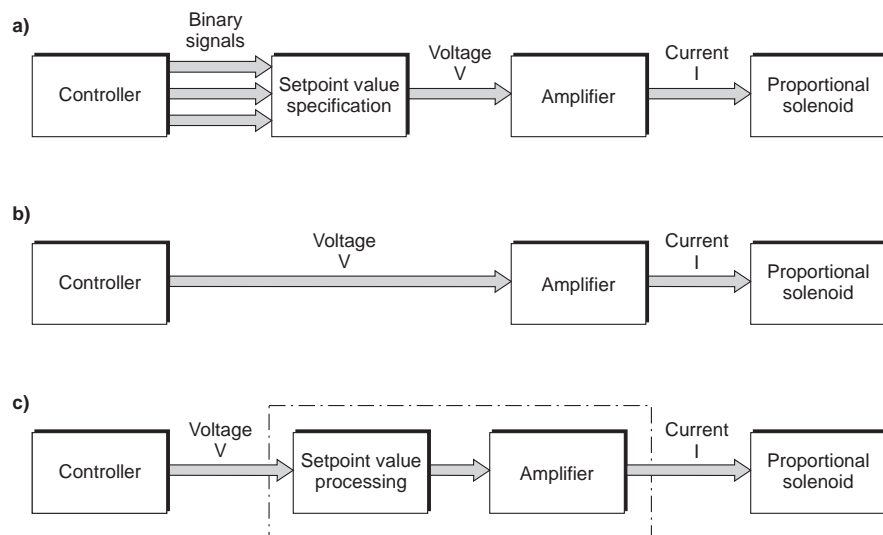


Fig. 4.2
Electronic modules
for signal flow
between controller and
proportional solenoid

With amplifiers for proportional valves, differentiation is made between two designs:

- The valve amplifier is built into the valve (integrated electronics)
- The valve amplifier is designed in the form of separate module or card (*fig. 1.6*).

Amplifier functions

Fig. 4.3a illustrates the three major functions of a proportional valve amplifier:

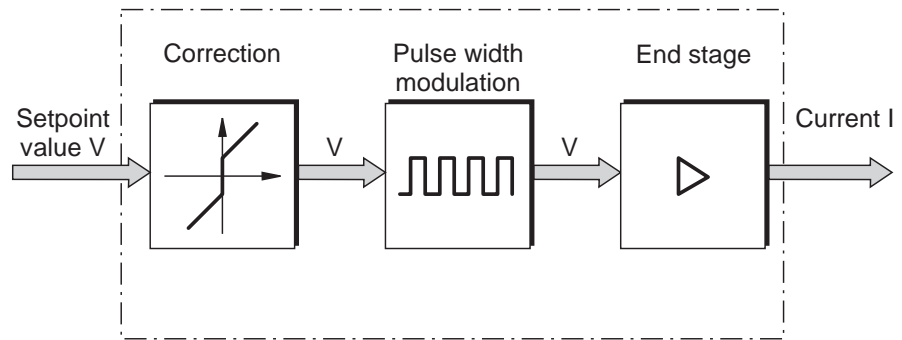
- Correcting element:
The purpose of this is to compensate the dead zone of the valve (see chapter. 4.2).
- Pulse width modulator:
This is used to convert the signal (= modulation).
- End stage:
This provides the required electrical capacity.

For valves with position controlled proportional solenoids, the sensor evaluation and the electronic closed-loop control are integrated in the amplifier (*fig. 4.3b*). The following additional functions are required:

- Voltage source:
This generates the supply voltage of the inductive measuring system.
- Demodulator:
The demodulator converts the voltage supplied by measuring system.
- Closed-loop controller:
In the closed-loop controller, a comparison is made between the prepared correcting variables and the position of the armature. The input signal for the pulse width modulation is generated according to the result.

4.1 Design and mode of operation of an amplifier

a) without positional control of the armature



b) with positional control of the armature

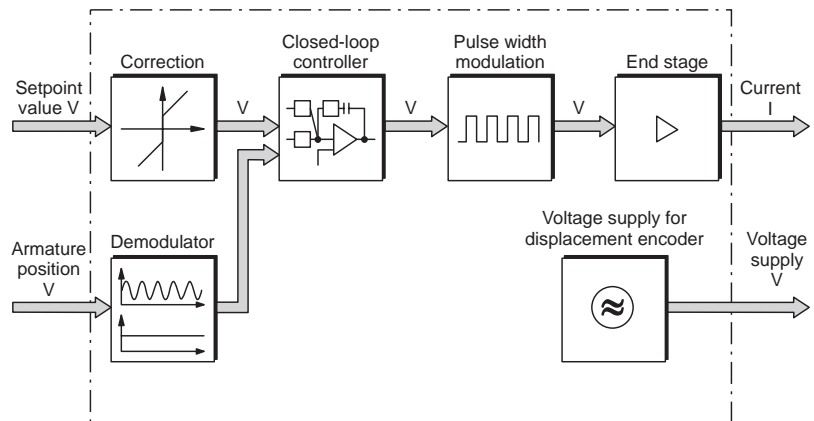


Fig. 4.3
Block diagrams for
one-channel amplifier

One and two-channel amplifier

A one-channel amplifier is adequate for valves with one proportional solenoid. Directional control valves actuated via two solenoids, require a two-channel amplifier. Depending on the control signal status, current is applied either to the lefthand or to the righthand solenoid only.

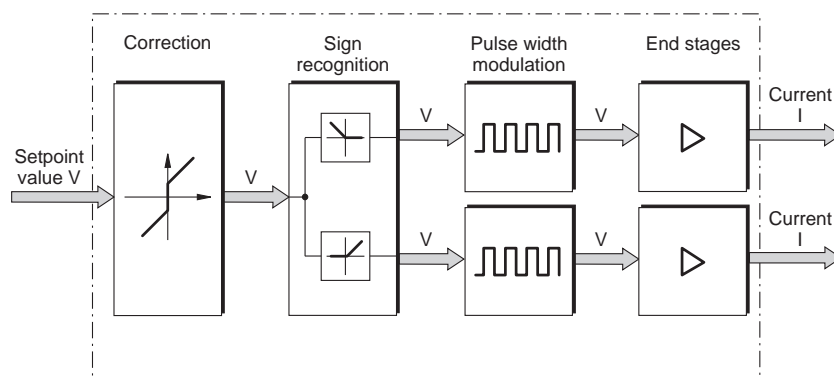


Fig. 4.4
Two-channel amplifier
(without positional control
of armature)

Pulse width modulation

Fig 4.5 illustrates the principle of pulse width modulation. The electrical voltage is converted into pulses. Approximately ten thousand pulses per second are generated.

When the end stage has been executed, the pulse-shaped signal acts on the proportional solenoid. Since the proportional solenoid coil inductivity is high, the current cannot change as rapidly as the electrical voltage. The current fluctuates only slightly by a mean value.

- A small electrical voltage as an input signal creates small pulses. The average current of the solenoid coil is small.
- The greater the electrical voltage, the wider the pulse. The average current through the solenoid coil increases.

The average current through the solenoid and the input voltage of the amplifier are proportional to one another.

Dither effect

The slight pulsating of the current as a result of the pulse width modulation causes the armature and valve spool to perform small oscillations at a high frequency. No static friction occurs. The response threshold, inversion range and hysteresis of the valve are clearly reduced.

The reduction in friction and hysteresis as a result of a high frequency signal is known as dither effect. Certain amplifiers permit the user to create an additional dither signal irrespective of pulse width modulation.

Heating of amplifier

As a result of pulse width modulation, three switching stages occur in end stage transistors:

- Lower signal value:
The transistor is inhibited. The power loss in the transistor is zero, since no current flows.
- Upper signal value:
The transistor is conductive. The transistor resistance in this status is very small and only a very slight power loss occurs.
- Signal edges:
The transistor switches over. Since the switch-over is very fast, power loss is very slight.

Overall, the power loss is considerably less than with an amplifier without pulse width modulation. The electronic components become less heated and the construction of the amplifier is more compact.

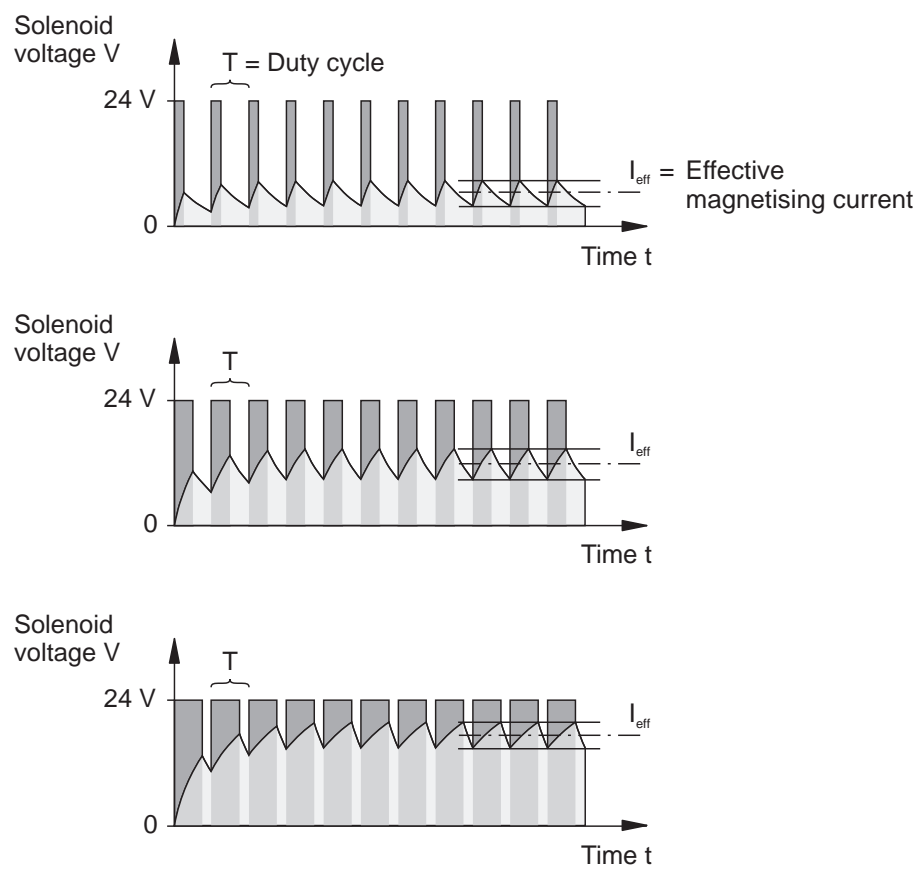


Fig. 4.5
Pulse width modulation

4.2 Setting an amplifier

Dead zone compensation

Fig. 4.6a illustrates the flow/signal characteristic for a valve with positive overlap. As a result of the overlap, the valve has a marked dead zone.

If you combine a valve and an amplifier with linear characteristic, the dead zone is maintained (fig. 4.6b).

If an amplifier is used with a linear characteristic as in fig. 4.6c, the dead zone can be compensated against this.

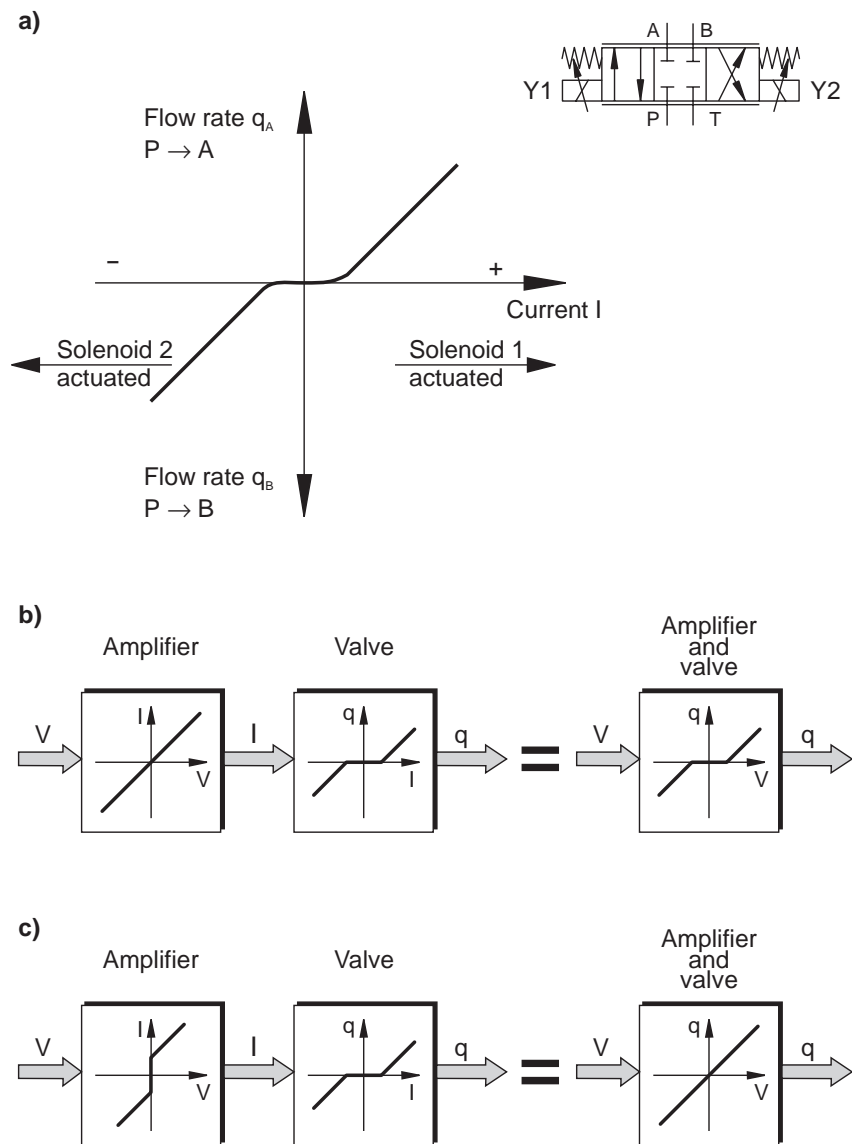


Fig. 4.6
Compensating
dead zone with a
proportional directional
control valve

Setting the amplifier characteristic

The valve amplifier characteristic can be set, whereby it is possible to

- use the same amplifier type for different valve types,
- compensate manufacturing tolerances within a valve series,
- replace only the valve or only the amplifier in the event of a fault.

The amplifier characteristic exhibits the same characteristics for valves by different manufacturers. However, the characteristic values are in some cases designated differently by various manufacturers and, accordingly, the setting instructions also vary.

Fig. 4.7 represents an amplifier characteristic for a two-channel amplifier. Solenoid 1 only is supplied with current for a positive control signal, and solenoid 2 only for a negative control signal.

Three variables are set:

- **Maximum current**

The maximum current can be adjusted in order to adapt the amplifier to proportional solenoids with different maximum current. With certain amplifiers, an amplification factor is set instead of the maximum current, which specifies the slope of the amplifier characteristic.

- **Jump current**

The jump current can be adjusted in order to compensate different overlaps. With various manufacturers, the jump current is set via a “signal characteriser”.

- **Basic current**

Due to manufacturing tolerances, the valve spool may not be exactly in the mid-position when both solenoids are de-energised. This error can be compensated by means of applying a basic current to one of the two proportional solenoids. The level of the basic current can be set. The term “offset setting” is often used to describe this compensating measure.

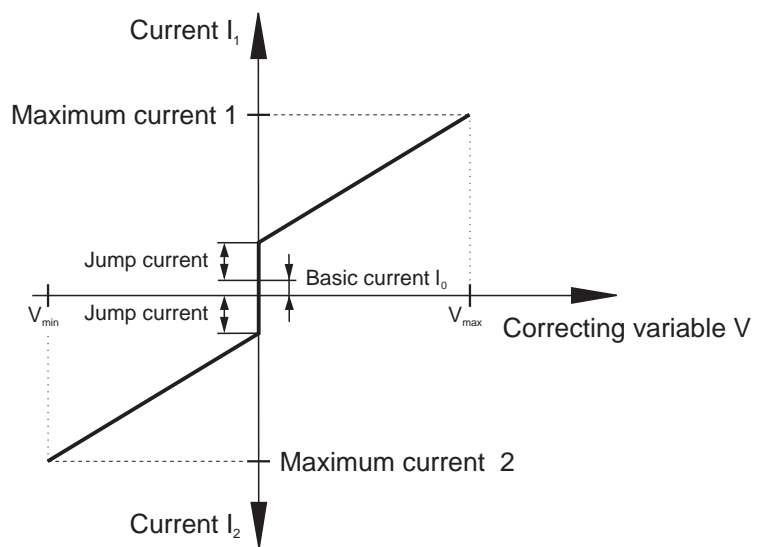


Fig. 4.7
Setting options with a
two channel
valve amplifier

An electrical voltage is required as a control signal (= setpoint value) for a proportional valve. The voltage can generally be varied within the following ranges:

- between 0 V and 10 V for pressure and restrictor valves,
- between -10 V and 10 V for directional control valves.

4.3 Setpoint value specification

The correcting variable y can be generated in different ways. Two examples are shown in (fig. 4.8).

- The potentiometer slide is moved by means of a hand lever. The correcting variable is tapped via the slide; this facilitates the remote adjustment of valves (fig. 4.8a).
- A PLC is used for the changeover between two setpoint values set by means of potentiometers (fig. 4.8b).

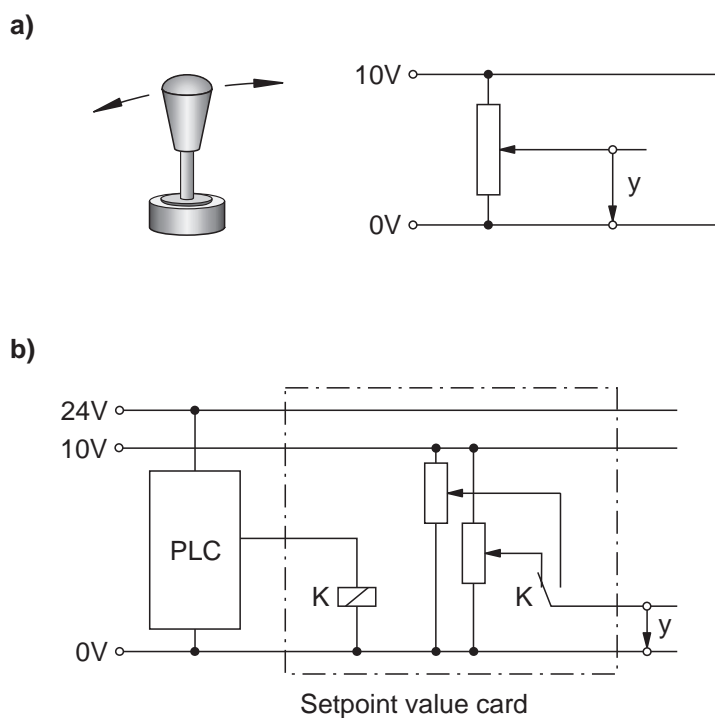


Fig. 4.8
Examples for setpoint value specification
a) Hand lever
b) Reversal via a PLC

Avoidance of pressure peaks and vibrations

Vibrations and pressure points are caused as a result of reversing a directional control valve. *Fig 4.9* compares three reversing variants.

A switching directional control valve only has the settings "valve open" and "valve closed". A change in the control signals leads to sudden pressure changes resulting in jerky acceleration and vibrations of the drive (*fig. 4.9a*).

With a proportional valve, it is possible to set different valve openings and speeds. With this circuit too, sudden changes in the control signal causes jerky acceleration and vibrations (*fig. 4.9b*).

To achieve a smooth, regular motion sequence, the correcting variable of the proportional valve is changed to a ramp form (*fig. 4.9c*).

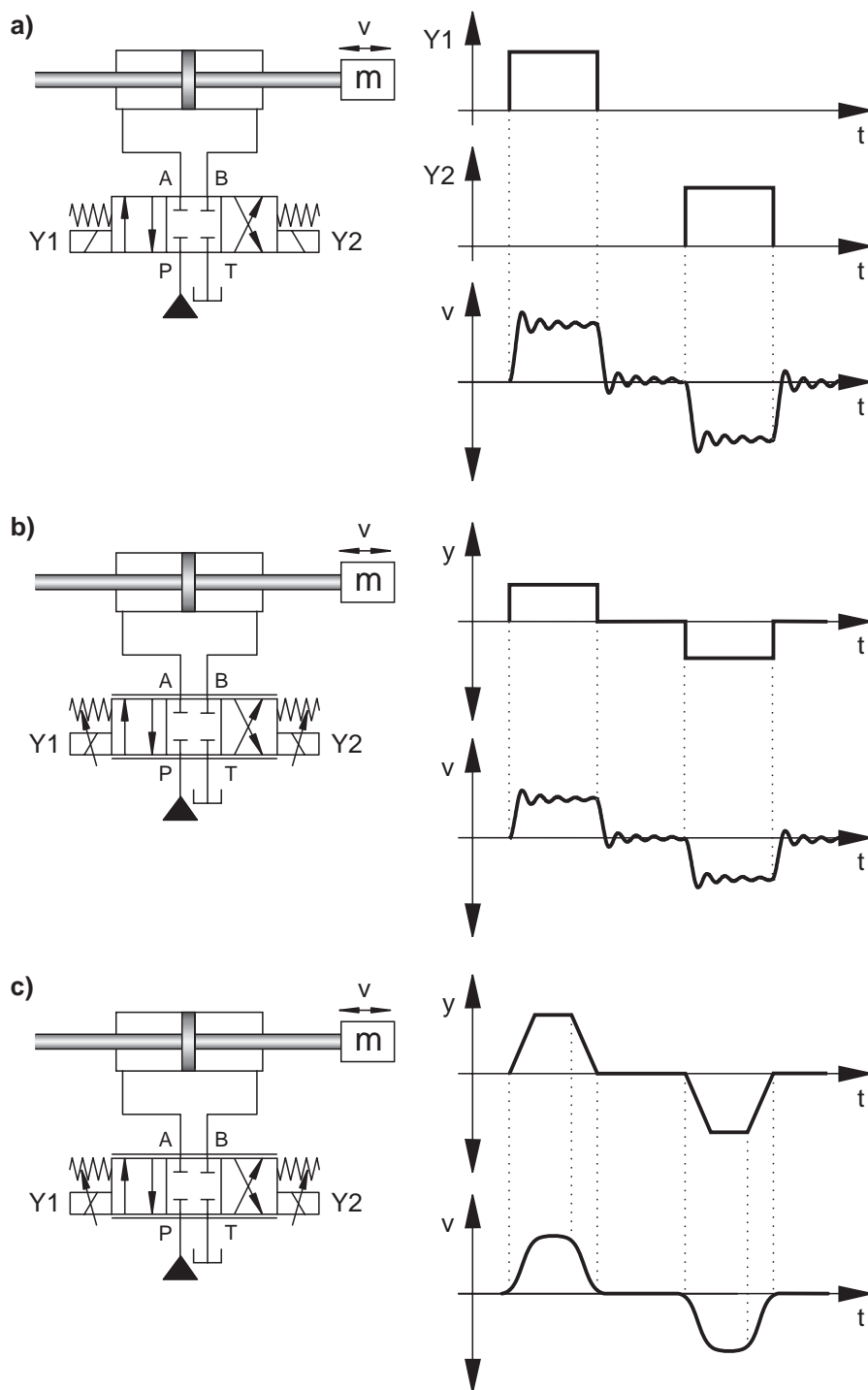


Fig. 4.9
Setpoint value specification and velocity of a cylinder drive

Different ramp slopes are frequently required for the retracting and advancing of a cylinder. Moreover, many applications also require different ramp slopes for the acceleration and deceleration of loads. For such applications, ramp shapers are used, which automatically recognise the operational status and changeover between different ramps.

Fig. 4.10 illustrates an application for various ramp slopes: a cylinder with unequal piston areas moving a load in the vertical direction.

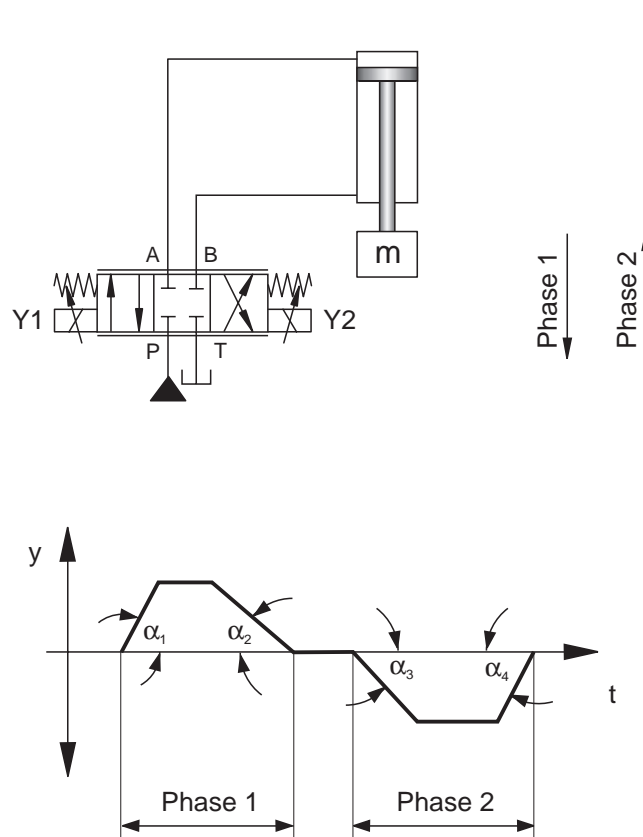


Fig. 4.10
Ramp shaper with
different
ramp slopes

Ramp shapers can be realised in different ways:

- built into the valve amplifier,
- with separate electronics connected between the controller and the valve amplifier,
- by means of programming a PLC with analogue outputs.

Chapter 5

Switching examples with proportional valves

Flow characteristics of proportional restrictors and directional control valves

The flow rate across the control edge of a proportional valve depends on the pressure drop. The following correlation applies between pressure drop and flow rate if the valve opening remains the same:

$$q \sim \sqrt{\Delta p}$$

This means: If the pressure drop across the valve is doubled, the flow rate increases by factor $\sqrt{2}$, i.e. to 141.4%.

Load-dependent speed control with proportional directional control valves

In the case of a hydraulic cylinder drive, the pressure drop across the proportional directional control valve falls, if the drive has to operate against force. Because of the pressure-dependency of the flow, the traversing speed also drops. This is to be explained by means of an example.

Let us consider the upwards movement of a hydraulic cylinder drive for two load cases:

- without load (*fig. 5.1a*),
- with load (*fig. 5.1b*).

The correcting variable is $4V$ in both cases, i.e.:
The valve opening is identical.

Without load, the pressure drop across each control edge of the proportional directional control valve is 40 bar. The piston of the drive moves upwards with speed $v = 0.2$ m/s (*fig. 5.1a*).

5.1 Speed control

If the cylinder has to lift a load, the pressure increases in the lower chamber, whilst the pressure in the upper chamber drops. Both these effects cause the pressure drop across the valve control edges to reduce, i.e. to 0 bar per control edge in the example shown.

The flow rate is calculated as follows:

$$\frac{q_{\text{with load}}}{q_{\text{without load}}} = \frac{\sqrt{\Delta p_{\text{with load}}}}{\sqrt{\Delta p_{\text{without load}}}} = \sqrt{\frac{1}{4}} = \frac{1}{2}$$

Speed and flow are proportional to one another. Consequently, the speed in the loaded state is calculated as follows:

$q \sim v$

$$\frac{v_{\text{with load}}}{v_{\text{without load}}} = \frac{q_{\text{with load}}}{q_{\text{without load}}} = \frac{1}{2}$$

$$v_{\text{with load}} = \frac{1}{2} v_{\text{without load}} = 0.1 \text{ m/s}$$

The speed is therefore considerably less than that without load despite identical valve opening.

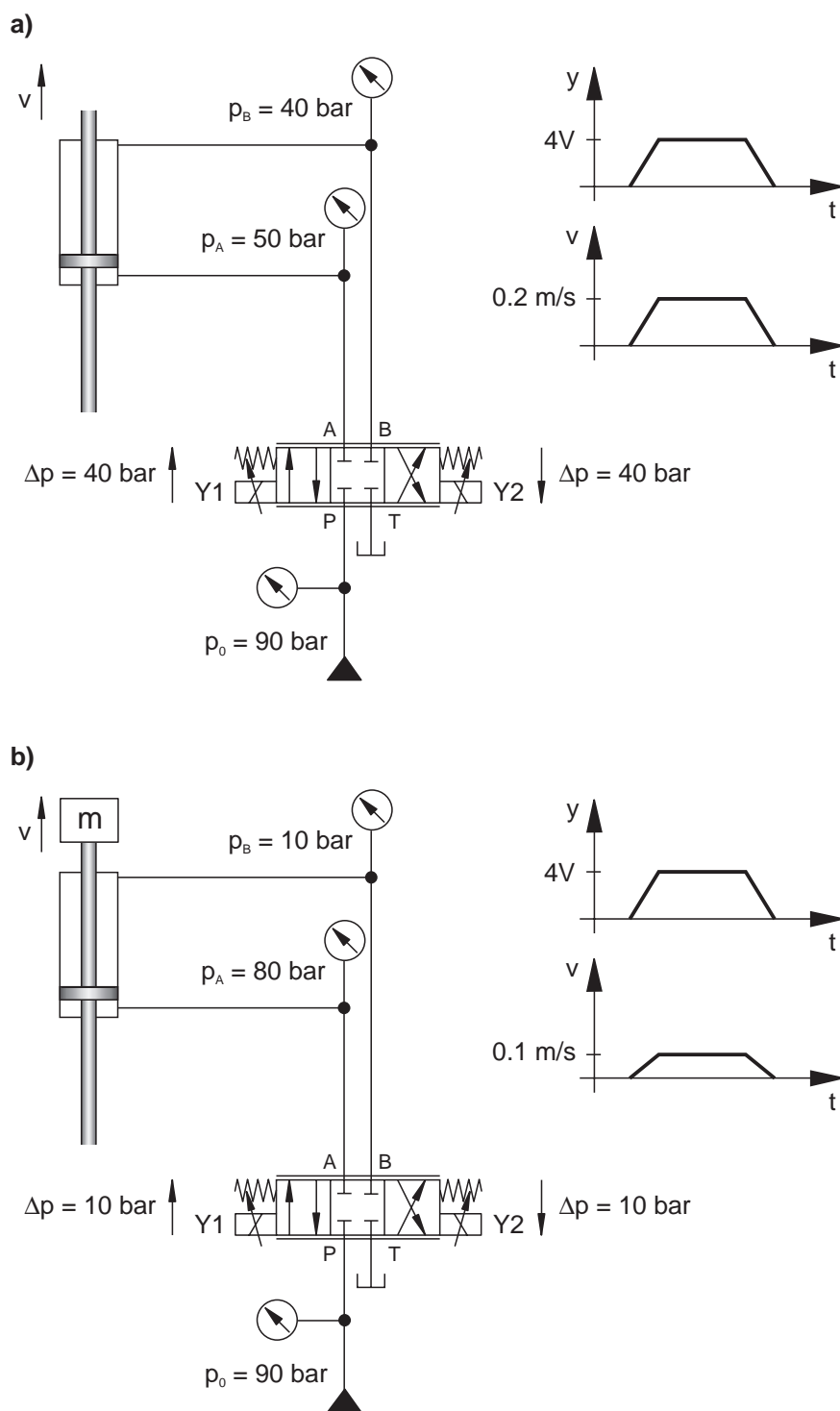


Fig. 5.1
Velocity of a
valve actuated cylinder
drive for two types of load
a) without load
b) with load

Load-independent speed control with proportional directional control valve and pressure balance

An additional pressure balance causes the pressure drop across the proportional directional control valve to remain constant irrespective of load. Flow and speed become load independent.

Fig 5.2 represents a circuit with feed pressure balance. The shuttle valve ensures that the higher of the two chamber pressures is always supplied to the pressure balance.

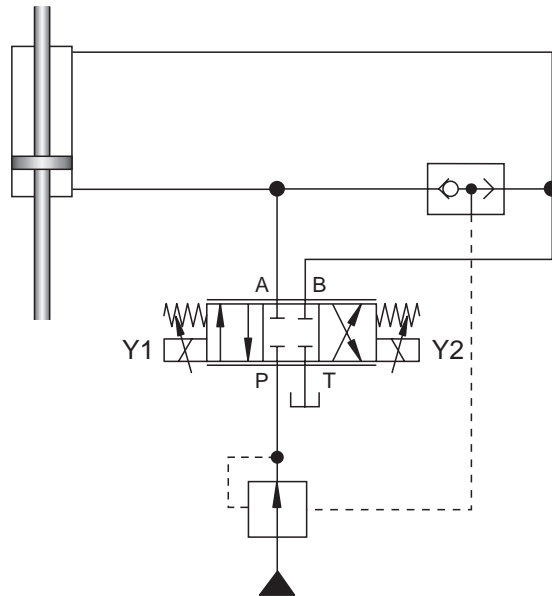


Fig. 5.2
Valve actuated cylinder
drive with supply pressure
balance

Differential circuit

With machine tools, two tasks are frequently required from hydraulic drives:

- fast feed speed for rapid traverse,
- high force and accurate, constant speed during working step.

Both requirements can be met by using the circuit shown in *fig. 5.3*.

- Extending the piston in rapid traverse causes the restrictor valve to open. The pressure fluid flows from the piston annular side through both valves to the piston side; the piston reaches a high speed.
- Extending the piston during the working step causes the restrictor valve to close. The pressure on the annular surface drops and the drive is able to exert a high force.
- Since the restrictor valve is in the form of a proportional valve, it is possible to changeover smoothly between rapid traverse and a working step.
- The restrictor valve remains closed during the return stroke.

Special 4/3-way proportional valves combining the functions of both valves are also used for differential circuits.

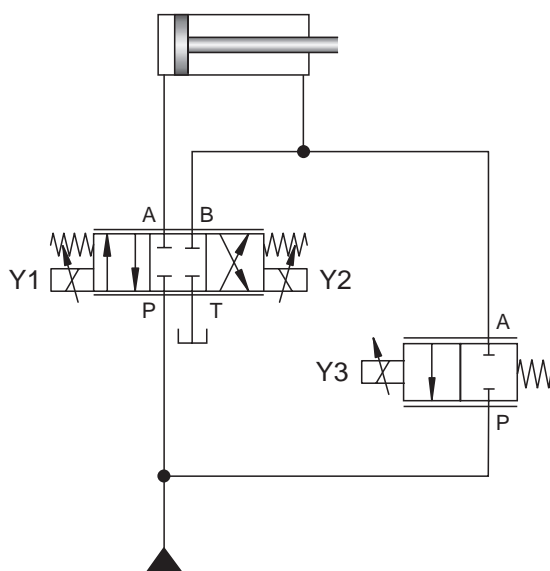


Fig 5.3
Differential circuit

Counter pressure

When decelerating loads, the pressure in the relieved cylinder chamber may drop below the ambient pressure. Air bubbles may be created in the oil as a result of the low pressure and the hydraulic system may be damaged due to cavitation.

The remedy for this is counter pressure via a pressure relief valve. This measure results in a higher pressure in both chambers and cavitation is eliminated.

The pressure relief valve is additionally pressurised with the pressure from the other cylinder chamber. This measure causes the opening of the pressure relief valve when the load is accelerated, thereby preventing the counter pressure having any detrimental in this operational status.

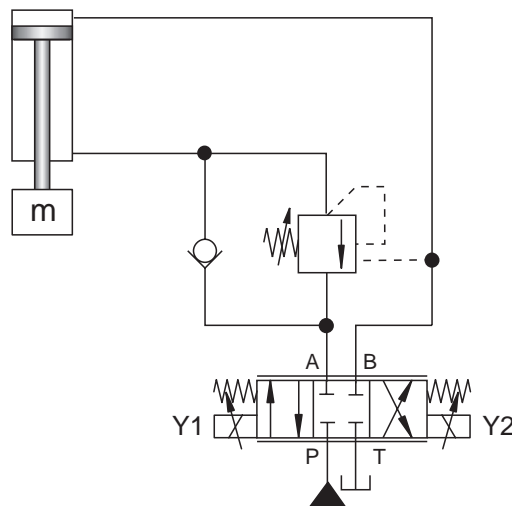


Fig. 5.4
Counter pressure with
pressure relief valve

Proportional restrictors and proportional directional control valves are available in the form of spool valves. With spool valves, a slight leakage occurs in the mid-position, which leads to slow “cylinder creep” with a loaded drive. It is absolutely essential to prevent this gradual creep in many applications, e.g. lifts.

5.2 Leakage prevention

In the case of an application, where the load must be maintained free of leakage, the proportional valve is combined with a poppet valve. *Fig. 5.5* illustrates a circuit with proportional directional control valve and a piloted, (delockable) non-return valve.

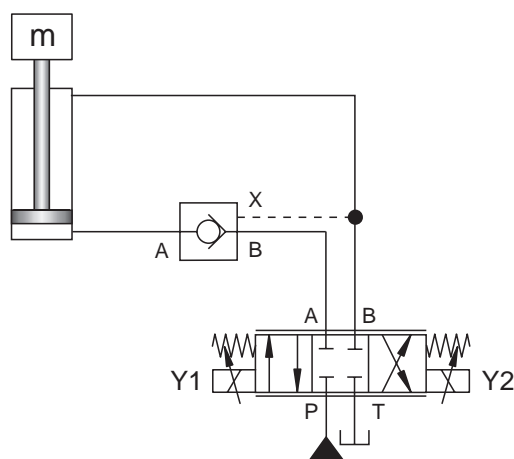


Fig. 5.5
Retention of a load using
a piloted non-return valve

Positioning drives are always used in those applications where loads have to be moved fast and accurately to a specific location. A lift is a typical example of an application for a hydraulic positioning drive. Cost-effective hydraulic positioning drives may be realised using proportional directional control valves and proximity sensors.

5.3 Positioning

Fig. 5.6a shows a circuit using a proximity sensor. Initially, the drive moves at a high speed owing to the large valve opening. After passing the sensor, the valve opening is reduced (ramp-shaper) and the drive decelerated. If the load is increased, this may lead to a distinct extension of the deceleration path and overtravelling of the destination position (*fig. 5.6a*)

Rapid traverse/creep speed circuit

A high positioning accuracy is obtained by means of a rapid traverse/creep speed circuit. After passing the first proximity sensor, the valve opening is reduced (ramp shaper) to a very small value. After passing the second proximity sensor, the valve is closed without ramp. Due to the reduced output speed for the second deceleration process, the position deviations for different loads are very slight (fig. 5.6b).

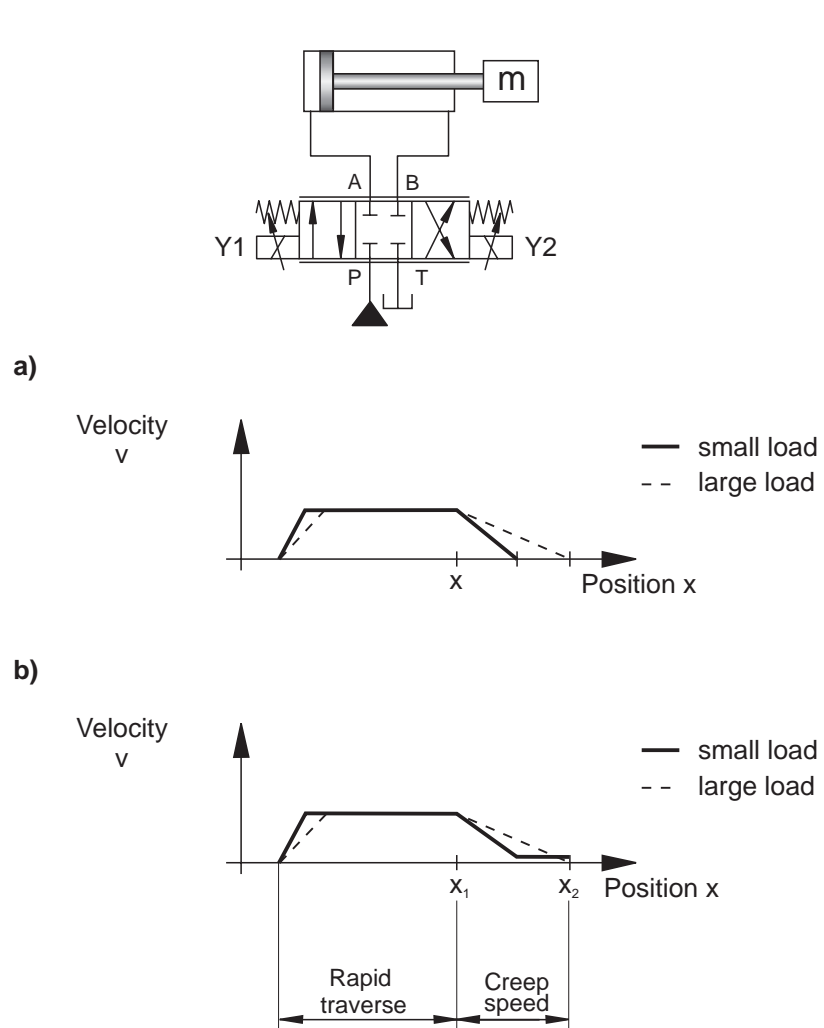


Fig. 5.6
Positioning with
rapid traverse/creep speed
circuit

Hydraulic drives are mainly used in applications, where large loads are moved and high forces generated. The power consumption and costs of a system are correspondingly high, which leaves room for a considerable potential saving in energy and cost.

Initially any measures to save energy by means of circuit technology represent an increase in the construction costs of a hydraulic system. However, by reducing power consumption, the additional costs usually can be very quickly recouped after a very short period of operation.

When movements are controlled by means of proportional valves, pressure drops via the control edges of the proportional valve. This leads to loss of energy and heating of the pressure medium.

Additional losses of energy may occur because the pump creates a higher flow rate than that required for the movement of the drive. The superfluous flow is vented to the tank via the pressure relief valve without performing a useful task.

Figs. 5.7 to 5.10 illustrate different circuit variants for a cylinder drive controlled by means of a proportional directional control valve. The following are represented for each circuit variant:

- the circuit diagram,
- the drive speed as a function of time (identical for all circuits, since the motion sequence of the drive is the same),
- the absorbed power of the pump as a function of time.

5.4 Energy saving measures

Fixed displacement pump, mid-position of directional control valve: closed

Fig. 5.7 illustrates a circuit, where the fixed displacement pump and the proportional directional control valve with mid-position closed are combined. The pump must be designed for the maximum required flow rate, continually supply this flow rate and deliver against the system pressure. Consequently, the resulting power consumption is correspondingly high.

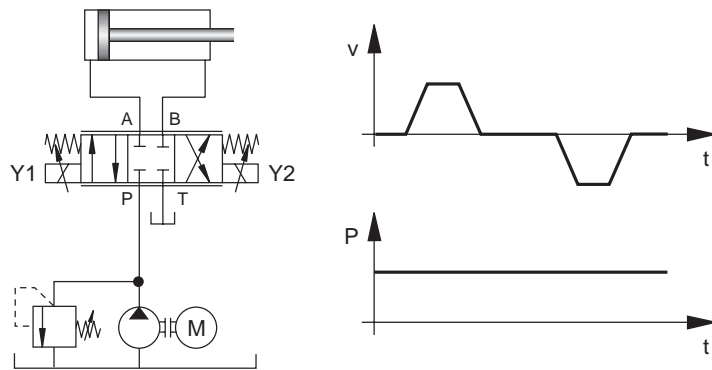


Fig. 5.7
Power consumption of a fixed displacement pump (mid-position of directional control valve: closed)

Fixed displacement pump, mid-position of directional control valve: Tank by-pass

A reduction in power consumption may be obtained by means of using a proportional valve with tank by-pass (fig. 5.8). Whilst the drive is stationary, the pump nevertheless supplies the full flow rate, but only needs to build up a reduced pressure, thus reducing the absorbed power during these phases accordingly. In the main, this leads to a lesser power consumption than that of the circuit shown in fig. 5.7.

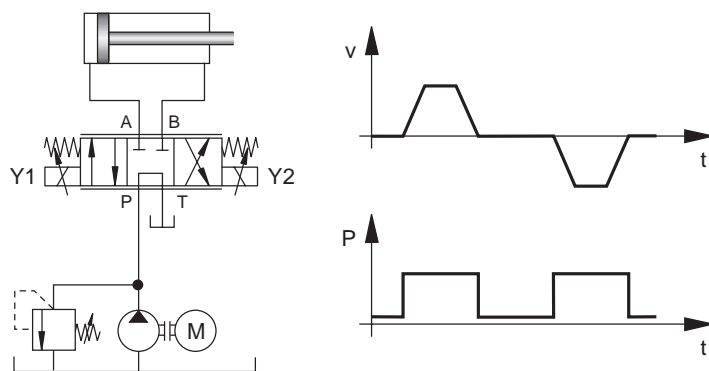


Fig. 5.8
Power consumption of a fixed displacement pump (mid-position of directional control valve: Tank by-pass)

Fixed displacement pump with reservoir

In many cases, the use of a valve with tank by-pass is not possible, since the pressure in the cylinder drops as a result of this. In such a case, a reservoir may be used (fig. 5.9). If the drive does not move at all or only slowly, then the pump loads the reservoir. In the rapid movement phases, part of the flow is supplied by the reservoir, whereby a smaller pump with a reduced delivery rate can be used. This leads to a reduction in absorbed power and power consumption.

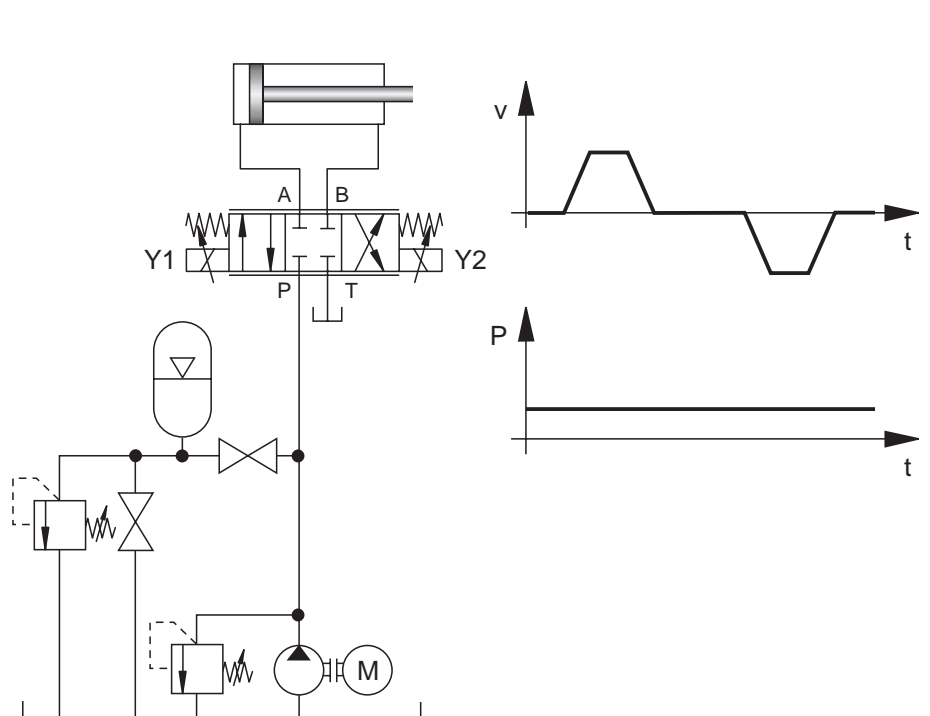


Fig. 5.9
Power consumption of a fixed displacement pump with additional reservoir (mid-position of directional control valve: closed)

Variable displacement pump

The variable displacement pump is driven at a constant speed. The input volume (= delivered oil volume per pump revolution) is adjustable, whereby the flow rate delivered by the pump is also changed.

The variable displacement pump is adjusted with two cylinders:

- The control cylinder with the larger piston area adjusts the pump in relation to higher flow rates.
- The control cylinder with the smaller piston area adjusts the pump in relation to smaller flow rates.

Pump regulation (circuit *fig. 5.10*) operates as follows:

- If the opening of the proportional directional control valve increases, the pressure at the pump output decreases. The switching valve of the pump regulator opens. The pump is driven by the control cylinder with the larger piston area and creates the required increased flow rate.
- If the opening of the directional control valve is reduced, the pressure rises at the pump output. Consequently, the 3/2-way valve switches. The control cylinder with the large piston area is connected with the tank. The pump reverts to the smaller control cylinder, resulting in a reduction in the flow rate. The absorbed power of the pump drops.
- With a closed valve, the flow rate and therefore the absorbed power of the pump is reduced down to zero. The absorbed power of the pump reverts to a very small value, which is required to overcome the frictional torque.

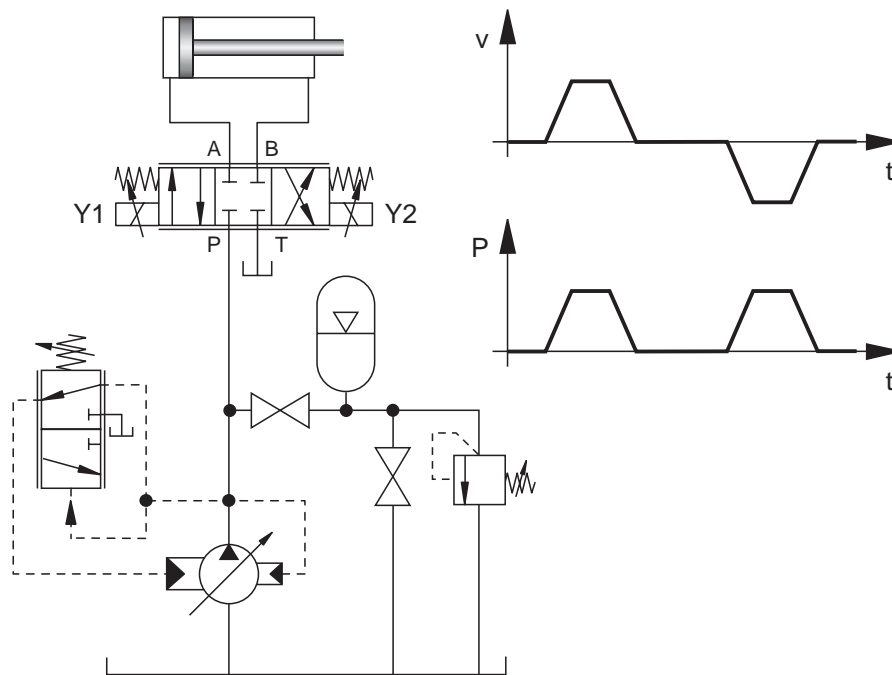


Fig. 5.10
Power consumption of a
variable displacement
pump
(mid-position of directional
control valve: closed)

The pressure relief valve is used merely for protection. The response pressure of this valve must be set higher than the working pressure of the pump. So long as the variable displacement pump operates fault-free, the valve remains closed.

If there is a sudden change in the valve opening, the pump cannot react sufficiently quickly. In this operating status a pressure reservoir is used as a buffer in order to prevent strong fluctuations in the supply pressure. Compared with the circuit shown in *fig. 5.9* a low pressure reservoir is adequate.

Comparison of power consumption between a fixed and a variable displacement pump

In contrast with the fixed displacement pump, the variable capacity pump only generates the flow rate actually required by the drive. Power losses are therefore minimised. The circuit using the variable displacement pump therefore displays the lowest power consumption.

Chapter 6

Calculation of motion characteristics of hydraulic cylinder drives

Hydraulic drives are able to generate high forces and move large loads. With the help of proportional valves, it is possible to control movements fast and accurately.

Depending on the application, either a linear cylinder, a rotary cylinder or a rotary motor are used. Linear cylinders are most frequently used. The following designs are therefore confined to this type of drive.

Drive systems with two cylinder types are taken into account:

1. Equal area, double-acting cylinder with through piston rod (fig. 6.1a):
Maximum force and maximum speed are identical for both directions of motion.
2. Unequal area, double-acting cylinder with single-ended piston rod (fig. 6.1b):
Maximum force and maximum speed vary for both motion directions.

The cylinder with single-ended piston rod is more cost effective and requires considerable less mounting space. It is therefore more often used in practice.

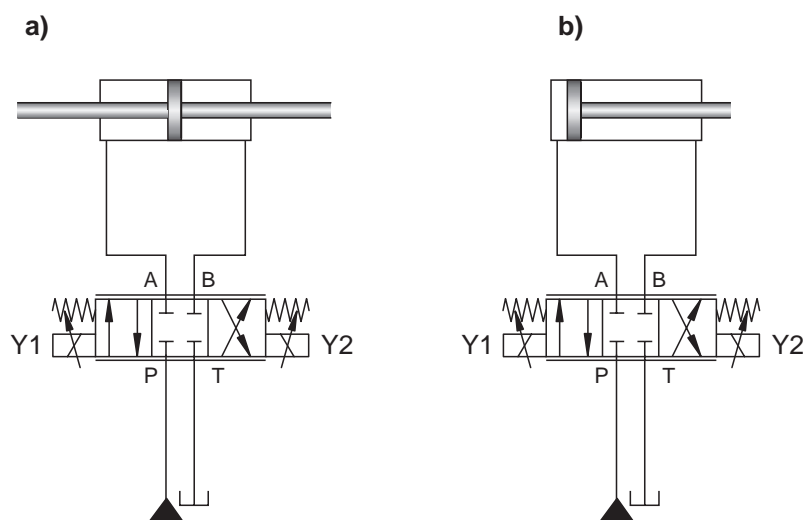


Fig. 6.1
Double-acting hydraulic
drive systems
a) with equal area
cylinder (double-ended
piston rod)
b) with unequal area
cylinder (single-ended
piston rod)

The performance data and the motion characteristics of a hydraulic cylinder drive can be roughly calculated. These calculations permit the following:

- to determine the duration of a motion sequence,
- to establish the correcting variable pattern,
- to select the required pump, the required proportional valve and the required cylinder.

Phases of a motion sequence

A simple motion sequence of a hydraulic drive consists of several phases (*fig. 6.2*):

- If the start and destination point of the motion are close together, the motion sequence comprises two phases: the acceleration phase (duration t_B , distance travelled x_B) and the delay phase (duration t_V , distance travelled x_V).
- If the start point and the destination point of the motion are sufficiently displaced, the motion sequence comprises three phases: the acceleration phase (duration t_B , distance travelled x_B), the phase with constant maximum speed (duration t_K , distance travelled x_K) and the delay phase (duration t_V , distance travelled x_V).

The duration of the overall motion is t_G . The piston rod of the drive travels the distance x_G .

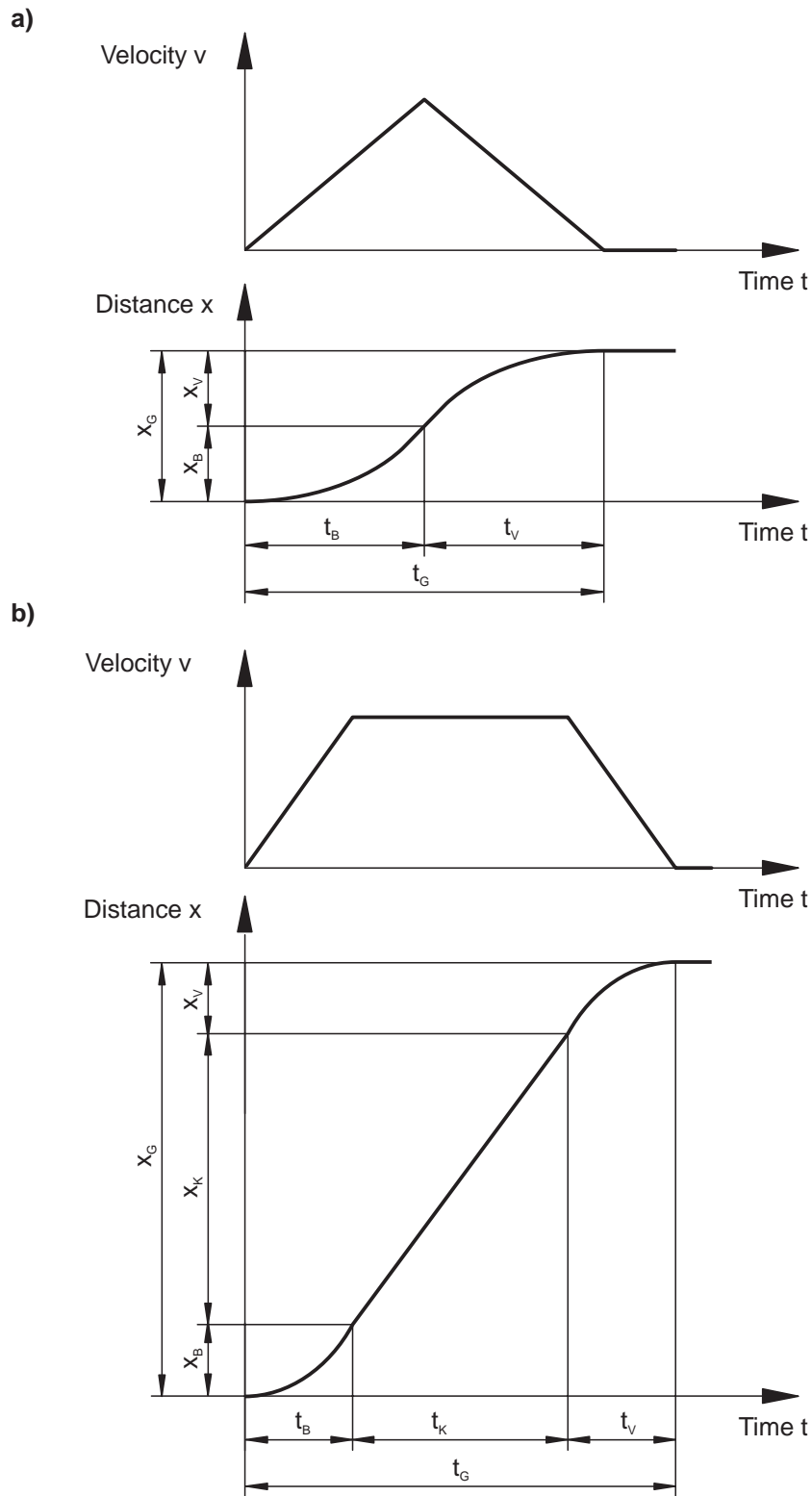


Fig. 6.2
Phases of a
motion sequence

Influencing factors on the duration of a motion sequence

In order for a motion sequence to be executed as fast as possible, the hydraulic drive system must achieve high acceleration, high delay and a high maximum velocity. Delay and maximum velocity are influenced by:

- the hydraulic system with pump, pressure relief valve, proportional directional control valve and cylinder,
- the load (forces and masses),
- the distance of start and destination point.

Table 6.1 provides a detailed breakdown of the influencing factors.

Hydraulic installation	
Cylinder	<ul style="list-style-type: none"> - Equal / unequal area - Stroke - Piston- / Annular area - Friction of seals
Proportional directional control valve	<ul style="list-style-type: none"> - Nominal flow - Flow/signal function
Energy supply using pump and pressure relief valve	<ul style="list-style-type: none"> - System pressure - Volumetric flow rate of pump
Load	
Mass load	<ul style="list-style-type: none"> - Mass - Motion direction (horizontal/vertical, inclined, upward / downward)
Load forces	<ul style="list-style-type: none"> - Pulling / pushing load - Friction in bearings, Guides
Distance of start and destination point	
	<ul style="list-style-type: none"> - small / large

Table 6.1
Factors influencing the
duration of a motion
sequence

Marginal conditions for calculation

Two assumptions have been made in order to simplify calculations:

- A 4/3-way proportional valve with four equal control edges and a linear flow/signal function is used.
- Prerequisite is a constant pressure system, i.e. the pump must be designed in such a way that it can still deliver the required flow rate even at maximum drive velocity.

With all calculations, the pressure is taken as standard pressure, i.e. the tank pressure is zero.

Nominal flow rate of a proportional directional control valve

The velocity, which can be attained by means of a hydraulic cylinder drive, depends on the nominal flow rate of the proportional directional control valve.

In the data sheet of a proportional directional control valve, the flow rate q_N is specified with full valve opening and a pressure drop of Δp_N per control edge.

Flow rate of a proportional directional control valve combined with a hydraulic drive

The operating conditions for the valve in a hydraulic drive system differ from the marginal conditions for measurement and the values for pressure and flow vary accordingly.

The flow range under the changed conditions is calculated according to *table 6.2*.

- The pressure drop across the control edge of the valve enters into the flow formula as a root value.
- With linear flow/signal function, the effect of the correcting variable is proportional to the valve opening and flow.

6.1 Flow rate calculation for proportional directional control valves

Table 6.2
Flow rate calculation

Valve parameters	<ul style="list-style-type: none"> - Nominal flow rate of proportional valve: q_N - Nominal pressure drop via a control edge of the proportional valve: Δp_N - maximum correcting variable of valve: y_{\max}
Operating conditions inside the hydraulic circuit	<ul style="list-style-type: none"> - actual pressure drop via a control edge of the proportional valve: Δp - actual correcting variable: y
Calculation for flow rate	$q = q_N \cdot \frac{y}{y_{\max}} \cdot \sqrt{\frac{\Delta p}{\Delta p_N}}$

Example 1 Flow calculation

The data for a 4/3-way proportional valve is as follows:

- Nominal flow: $q_N = 20 \text{ l/min}$, measured with a pressure drop of $\Delta p_N = 5 \text{ bar}$. The nominal flow rate is equal for all four control edges.
- maximum control signal: $y_{\max} = 10 \text{ V}$
- linear flow/signal function

A proportional valve is used in a hydraulic drive system. The following values were measured during the advancing of the piston rod:

- Control signal: $y = 4 \text{ V}$.
- Pressure drop across the inlet control edge: $\Delta p_A = 125 \text{ bar}$.

Required

the flow rate q_A via the inlet control edge of the valve under the given conditions

- **Flow rate calculation**

$$\begin{aligned}
 q_A &= q_N \cdot \frac{y}{y_{\max}} \cdot \sqrt{\frac{\Delta p_A}{\Delta p_N}} \\
 &= 20 \frac{\text{l}}{\text{min}} \cdot \frac{4\text{V}}{10\text{V}} \cdot \sqrt{\frac{125 \text{ bar}}{5 \text{ bar}}} \\
 &= 20 \frac{\text{l}}{\text{min}} \cdot 0,4 \cdot 5 = 40 \frac{\text{l}}{\text{min}}
 \end{aligned}$$

Chamber pressures and pressure drop across the control edges

A cylinder drive with equal areas is being considered, which is not connected to a load (fig. 6.3). Friction and leakage are disregarded. The valve opening is constant and the piston rod moves at a constant speed. Half the supply pressure builds up in both chambers. The differential pressure Δp_A across the inlet control edge is identical to the differential pressure Δp_B across the outlet control edge. The value of both differential pressures is $p_0/2$.

6.2 Velocity calculation for a cylinder drive with equal areas disregarding load and frictional forces.

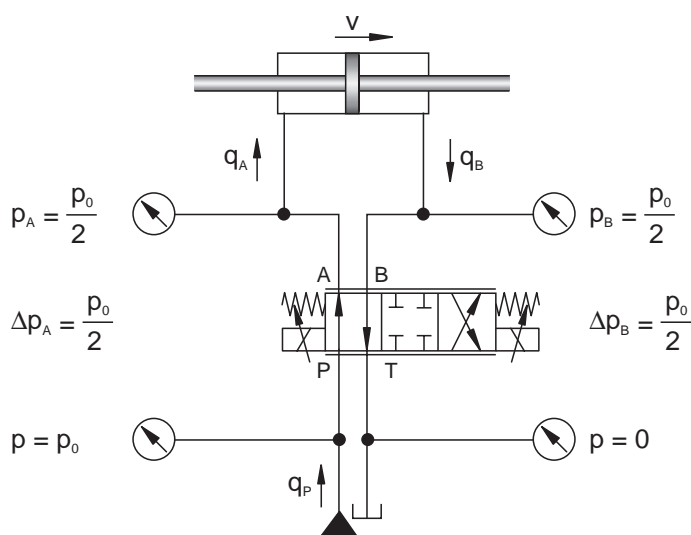


Fig. 6.3 Chamber pressures and differential pressures across the control edges with an equal area cylinder drive (disregarding load and frictional forces)

Velocity calculation

The calculation formulae for velocity are listed in *table 6.3*.

- The effective piston annular area is the result of the difference between the piston area and the piston rod area.
- The flow rate via a valve control edge is calculated as shown in *table 6.2*.
- To calculate the velocity, the flow rate across a valve control edge is divided by the piston annular area.

Sizing the pump

The pump must be able to deliver the flow rate flowing across the inlet control edge with the maximum valve opening.

Parameters of the hydraulic drive system	
Energy supply	Supply pressure: p_0
Valve	see table 6.2
Cylinder	Piston diameter: D_K Rod diameter: D_S
Calculation formulae	
Annular area	$A_R = \frac{\pi}{4} \cdot (D_K^2 - D_S^2)$
Flow rate via a control edge	$q_A = q_B = q_N \cdot \frac{y}{y_{\max}} \cdot \sqrt{\frac{p_0}{2 \cdot \Delta p_N}}$
Velocity	$v = \frac{q}{A_R}$
Volumetric flow rate of pump	$q_P = q_{A_{\max}} = q_N \cdot \frac{y_{\max}}{y_{\max}} \cdot \sqrt{\frac{p_0}{2 \cdot \Delta p_N}} = q_N \cdot \sqrt{\frac{p_0}{2 \cdot \Delta p_N}}$

Table 6.3
Velocity calculation for an equal area cylinder drive disregarding load and frictional forces

Velocity calculation for an equal area cylinder drive disregarding load and frictional forces

Example 2

A hydraulic drive system consists of the following components:

- a proportional directional control valve with identical data to *example 1*,
- an equal area cylinder
piston diameter: $D_K = 100$ mm,
piston rod diameter: $D_S = 70.7$ mm,
- a constant pump,
- a pressure relief valve
set system pressure: $p_0 = 250$ bar.

Required

- the maximum velocity of the drive (correcting variable $y_{\max} = 10$ V)
- the velocity of the drive for a correcting variable $y = 2$ V
- the flow rate q_P , to be delivered by the pump

- **Calculation of piston annular area**

$$A_R = \frac{\pi}{4} \cdot (100^2 - 70.7^2) \text{ mm}^2 = 3928 \text{ mm}^2 = 39.3 \text{ cm}^2$$

- **Calculation of maximum velocity**

Flow via a control edge with maximum correcting variable

$$q_{A_{\max}} = q_N \cdot \sqrt{\frac{p_0}{2 \cdot \Delta p_N}} = 20 \frac{\text{l}}{\text{min}} \cdot \sqrt{\frac{250 \text{ bar}}{2 \cdot 5 \text{ bar}}} = 100 \frac{\text{l}}{\text{min}}$$

Maximum velocity

$$\begin{aligned} v_{\max} &= \frac{q_{A_{\max}}}{A_R} = \frac{100 \frac{\text{l}}{\text{min}}}{39.3 \text{ cm}^2} = \frac{100 \text{ dm}^3}{60 \text{ s} \cdot 0.393 \text{ dm}^2} \\ &= 4.24 \frac{\text{dm}}{\text{s}} = 42.4 \frac{\text{cm}}{\text{s}} \end{aligned}$$

■ **Velocity calculation with a correcting variable of 2 V**

Flow via a control edge with a correcting variable of 2 V:

$$q_A = q_N \cdot \frac{y}{y_{\max}} \cdot \sqrt{\frac{p_0}{2 \cdot \Delta p_N}} = 20 \frac{\text{l}}{\text{min}} \cdot \frac{2 \text{ V}}{10 \text{ V}} \cdot \sqrt{\frac{250 \text{ bar}}{2 \cdot 5 \text{ bar}}} = 20 \frac{\text{l}}{\text{min}}$$

Velocity with a correcting variable of 2 V

$$v = \frac{q_A}{A_R} = \frac{20 \frac{\text{l}}{\text{min}}}{39.3 \text{ cm}^2} = \frac{20 \text{ dm}^3}{60 \text{ s} \cdot 0.393 \text{ dm}^2} = 8.48 \frac{\text{cm}}{\text{s}}$$

■ **Calculation of the required pump flow**

$$q_P = q_{A_{\max}} = 100 \frac{\text{l}}{\text{min}}$$

Area ratio of an unequal area cylinder drive

With an unequal area cylinder drive, the pressure in one chamber acts on the piston area and in the other chamber on the piston annular area. The ratio of piston area to piston annular area is known as the area ratio α (table 6.4). With a unequal area cylinder, the area ratio α is greater than 1.

6.3 Velocity calculation for an unequal area cylinder drive disregarding load and frictional forces

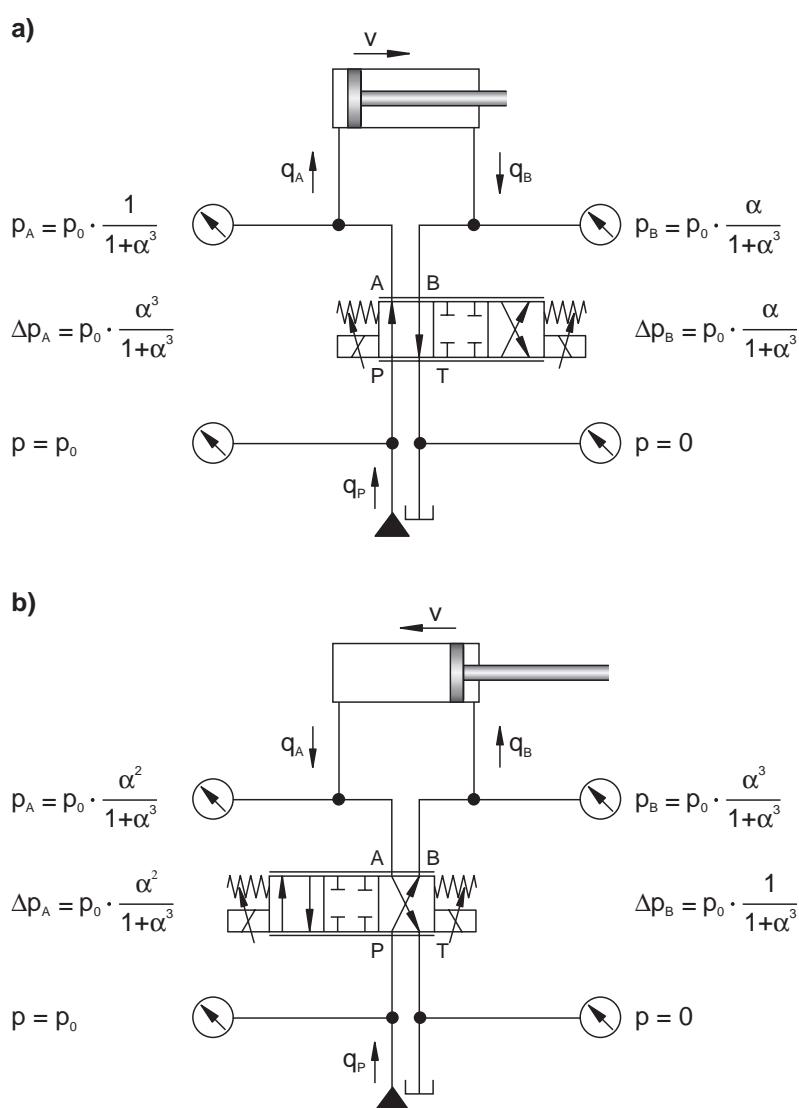


Fig. 6.4 Chamber pressures and differential pressures across the control edges using an unequal area cylinder drive (disregarding load and frictional forces)
 a) Advancing of piston rod
 b) Returning of piston rod

Advance sequence:

Chamber pressures and pressure drop across the valve control edges

The pressure in the cylinder chambers and the differential pressures across the control edges are determined by the force equilibrium at the piston and the root valve flow characteristics. Advancing of the piston rod results in the following correlations (*fig. 6.4a*):

- Force equilibrium at the piston:
Since there is no load, the forces on both sides of the piston are identical. The pressure on the piston annular area is greater by factor α than the pressure on the piston area.
- Flow characteristics:
The piston area is greater by the factor α than the piston annular area. Accordingly, the flow via the inlet control edge is α times greater than that via the outlet control edge. Since the flow only increases with the pressure drop in root value, the pressure drop Δp_A across the inlet control edge is greater by the factor α^2 than the pressure drop Δp_B across the outlet control edge.

The pressures and differential pressures listed in *fig. 6.4a* can be calculated from the conditions for force equilibrium and flow.

Retract sequence:

Chamber pressures and pressure drop across the valve control edges

During retracting, the flow via the inlet control edge is reduced by the factor α than the flow via the outlet control edge. The pressures and differential pressures entered in *fig. 6.4b* obtained by taking into account the force equilibrium at the piston and the flow ratio.

Velocity calculation

The formulae for the calculation of velocity for the advancing and retracting of the piston rod are listed in *table 6.4*.

The velocity for advancing the piston is determined in two steps.

- Flow calculation for the inlet control edge:
The pressure drop across the inlet control edge Δp_A in *fig. 6.4a* is entered in the flow formula (*table 6.2*).
- Velocity calculation:
The flow rate via the inlet control edge is divided by the piston area.

The process of calculating the return velocity is also carried out in two steps. In order to calculate the flow via the inlet control edge, the pressure drop Δp_B according to *fig 6.4b* is applied in the flow ratio according to *table 6.2*. The velocity is calculated by dividing the flow value by the piston annular area.

Sizing the pump

During the advancing of the piston rod the flow rate via the inlet control edge is greater by factor $\alpha^{1,5}$ than during returning (*table 6.4*). The maximum flow rate during advancing must therefore be used as a basis for the sizing of the pump. This occurs with the maximum valve opening.

Parameters of the hydraulic drive system	
	see table 6.3
Cylinder calculation formulae	
Piston area	$A_K = \frac{\pi}{4} \cdot D_K^2$
Area ratio	$\alpha = \frac{A_K}{A_R} = \frac{D_K^2}{D_K^2 - D_S^2}$
Calculation formulae for advancing of piston rod	
Flow rate via inlet control edge	$q_A = q_N \cdot \frac{y}{y_{\max}} \cdot \sqrt{\frac{\Delta p_A}{\Delta p_N}} = q_N \cdot \frac{y}{y_{\max}} \cdot \sqrt{\frac{p_0 \cdot \alpha^3}{\Delta p_N \cdot (1 + \alpha^3)}}$
Advance velocity of piston rod	$v = \frac{q_A}{A_K} = \frac{q_N}{A_K} \cdot \frac{y}{y_{\max}} = \sqrt{\frac{p_0 \cdot \alpha^3}{\Delta p_N \cdot (1 + \alpha^3)}}$
Calculation formulae for returning of piston rod	
Flow rate via inlet control edge	$q_B = q_N \cdot \frac{y}{y_{\max}} \cdot \sqrt{\frac{\Delta p_B}{\Delta p_N}} = q_N \cdot \frac{y}{y_{\max}} \cdot \sqrt{\frac{\Delta p_0}{\Delta p_N \cdot (1 + \alpha^3)}}$
Return velocity of piston rod	$v = \frac{q_B}{A_R} = \frac{q_B \cdot \alpha}{A_K} = \frac{q_N}{A_K} \cdot \frac{y}{y_{\max}} \cdot \sqrt{\frac{p_0 \cdot \alpha^2}{\Delta p_N \cdot (1 + \alpha^3)}}$
Calculation formulae for volumetric flow rate of pump	
	$q_P = q_{\max} = q_N \cdot \frac{y_{\max}}{y_{\max}} \cdot \sqrt{\frac{p_0 \cdot \alpha^3}{\Delta p_N \cdot (1 + \alpha^3)}}$ $= q_N \cdot \sqrt{\frac{p_0 \cdot \alpha^3}{\Delta p_N \cdot (1 + \alpha^3)}}$

Table 6.4
Velocity calculation for an unequal area cylinder drive disregarding load and frictional forces

Comparison of return and advance velocity for a cylinder drive using a 4/3-way proportional valve

If the pump is correctly sized, it delivers under any conditions at least the maximum flow rate q_{\max} able to flow via the inlet control edge of the proportional directional control valve with the supply pressure p_{\max} . Under this condition, pressure p_0 always applies at port P of the proportional directional control valve. The drive with proportional control valve may be regarded as a constant pressure system (*table 6.5*).

With a constant pressure system, the valve opening is the critical factor for velocity, and the advance velocity of an unloaded, unequal area cylinder drive is greater by the factor than its return velocity (*table 6.4*).

Comparison of return and advance velocity for a cylinder drive using a 4/3-way switching valve

If a hydraulic cylinder drive is controlled by a switching 4/3-way valve, then the velocity is limited by the volumetric flow rate of the pump. A constant flow system is used (*table 6.5*).

With a constant flow system, the return velocity of an unequal area cylinder drive is greater by factor α than the advance velocity.

	Constant pressure system	Constant flow system
Valve type	4/3-way proportional valve	4/3-way switching valve
Constant	Pressure at port P of the 4/3-way proportional valve (corresponds to supply pressure p_0)	Volumetric flow rate q_A via the inlet opening of the valve (corresponds to volumetric flow rate q_p of pump)
Variable	Flow rate q_A via inlet control edge (depends on load and correcting variable)	Pressure at port P of directional control valve (depends on load)
Volumetric flow rate via the pressure relief valve	In almost all points of operation q_A is less than q_p . The remaining volumetric flow rate exhausts via the pressure relief valve.	With constant motion velocity
Velocity of an unequal area cylinder	Advance velocity greater than return velocity	Return velocity greater than advance velocity

Table 6.5
Comparison of a constant pressure system and a constant flow system

Example 3 Velocity calculation for an unequal area cylinder drive disregarding load and frictional forces

The data for the pressure supply and the proportional directional control valve is the same as that in *example 2*. The piston and piston rod diameter are also identical.

Required

- the maximum advance velocity of the piston rod (control variable: $y = 10 \text{ V}$)
- the maximum return velocity of the piston rod (control variable: $y = -10 \text{ V}$)
- the required volumetric flow rate of the pump q_p

■ Calculation of the cylinder

Piston area

$$A_K = \frac{\pi}{4} \cdot D_K^2 = \frac{\pi}{4} \cdot 100^2 \text{ mm}^2 = 7854 \text{ mm}^2 = 0.785 \text{ dm}^2$$

Area ratio

$$\alpha = \frac{A_K}{A_R} = \frac{7854 \text{ mm}^2}{3928 \text{ mm}^2} = 2$$

■ Calculation of the maximum advance velocity

Flow rate via the inlet control edge

$$\begin{aligned} q_A &= q_N \cdot \frac{y}{y_{\max}} \cdot \sqrt{\frac{p_0}{\Delta p_N} \cdot \frac{\alpha^3}{1 + \alpha^3}} \\ &= 20 \frac{\text{l}}{\text{min}} \cdot \frac{10 \text{ V}}{10 \text{ V}} \cdot \sqrt{\frac{250 \text{ bar}}{5 \text{ bar}} \cdot \frac{8}{9}} = 133.3 \frac{\text{l}}{\text{min}} \end{aligned}$$

maximum advance velocity

$$v = \frac{q_A}{A_K} = \frac{133.3 \text{ dm}^3}{60 \text{ s} \cdot 0.785 \text{ dm}^2} = 2.8 \frac{\text{dm}}{\text{s}} = 0.28 \frac{\text{m}}{\text{s}}$$

■ Calculation of the maximum return velocity

Flow rate via the inlet control edge

$$\begin{aligned} q_B &= q_N \cdot \frac{y}{y_{\max}} \cdot \sqrt{\frac{p_0}{\Delta p_N} \cdot \frac{1}{1 + \alpha^3}} \\ &= 20 \frac{\text{l}}{\text{min}} \cdot \sqrt{\frac{250 \text{ bar}}{5 \text{ bar} \cdot 9}} = 47.1 \frac{\text{l}}{\text{min}} \end{aligned}$$

maximum return velocity

$$v = \frac{q_B}{A_R} = \frac{q_B \cdot \alpha}{A_K} = \frac{47.1 \text{ dm}^3 \cdot 2}{60 \text{ s} \cdot 0.785 \text{ dm}^2} = 2 \frac{\text{dm}}{\text{s}} = 0.2 \frac{\text{m}}{\text{s}}$$

■ Calculation of the required volumetric flow rate of the pump

$$q_P = q_{\max} = q_N \cdot \sqrt{\frac{p_0}{\Delta p_N} \cdot \frac{\alpha^3}{1 + \alpha^3}} = 133.3 \frac{\text{l}}{\text{min}}$$

6.4 Velocity calculation for an equal area cylinder drive taking into account load and frictional forces

Maximum force of the drive piston

The maximum force F_{\max} acts on the piston, if supply pressure prevails in one chamber of the hydraulic cylinder and in the other, tank pressure. The maximum force for an equal area cylinder drive is calculated as a product of supply pressure and piston annular area (table 6.6).

Piston force with constant motion velocity

With constant motion velocity, the actual piston force F is made up of the load force F_L and the frictional force F_R , whereby the following sign definitions are to be observed:

- A load force acting against the motion is described as a pushing load and is to be used with a positive sign.
- A load force acting in the direction of the motion, i.e. supporting the motion sequence, is described as a pulling load and is to be used with a negative sign.
- The frictional force always acts against the motion and must therefore always be used with a positive sign.

In order for the piston to always move in the desired direction, the piston force F must always be less than the maximum piston force F_{\max} .

Load pressure, chamber pressure and differential pressure across the control edges

The load pressure p_L indicates which differential pressure is to prevail between the two cylinder chambers in order to generate force F . This is calculated for the equal area cylinder drive by dividing the piston force F by the piston annular area A_R . By taking into account the load pressure, the pressure and differential pressures shown in fig. 6.5 occur.

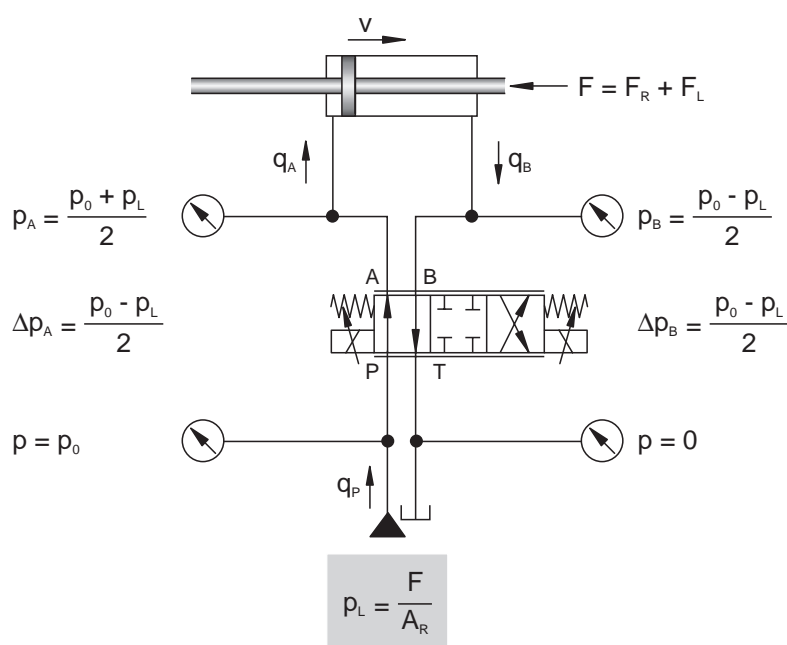


Fig. 6.5
Chamber pressures and differential pressures across the control edges with an equal area cylinder drive (with load and frictional force)

Parameters of the hydraulic drive system	
	see table 6.3
Parameters of load	
Load force	F_L
Frictional force	F_R
Calculation formulae for forces and load pressure	
Maximum piston force	$F_{\max} = A_R \cdot p_0$
Actual piston force	$F = F_L + F_R$
Load pressure	$p_L = \frac{F}{A_R}$
Calculation formulae for velocity, direct for loaded drive	
Flow rate across a control edge	$q_A = q_B = q_N \cdot \frac{y}{y_{\max}} \cdot \sqrt{\frac{p_0 - p_L}{2 \cdot \Delta p_N}}$
Velocity with load	$v_L = \frac{q_A}{A_R}$
Calculation formulae for velocity, from unloaded drive	
Velocity without load	v calculated according to table 6.3
Velocity	$v_L = v \cdot \sqrt{\frac{p_0 - p_L}{p_0}} = v \cdot \sqrt{\frac{F_{\max} - F}{F_{\max}}}$
Calculation formulae for volumetric flow rate of pump	
	$q_P = q_{A_{\max}} = q_N \cdot \sqrt{\frac{p_0 - p_L}{2 \cdot \Delta p_N}}$

Table 6.6
Velocity calculation for an
equal area cylinder
(with load and frictional
force)

Calculation of motion velocity

The motion velocity is calculated in two steps (*table 6.6*):

- Flow rate calculation:
Flow rates q_A and q_B are identical. These are determined by including the differential pressure Δp_A or Δp_B (*fig. 6.5*) in the flow ratio (*table 6.2*).
- Velocity calculation
The flow rate q_A is divided by the piston annular area A_R .

If the motion velocity of the unloaded drive has already been established, then it is expedient to determine the velocity v_L under load influence from the premise of the velocity of the unloaded drive (*table 6.6*).

Pump sizing

Since the required volumetric flow rate q_A increases with the increasing motion velocity of the drive, the pump sizing is according to the motion direction with the higher velocity. With a pulling load, the load acts in the direction of motion and the load force F_L is negative. Under this marginal condition, the velocity of the piston and the required volumetric flow rate q_P of the pump can become higher than in the load-free state.

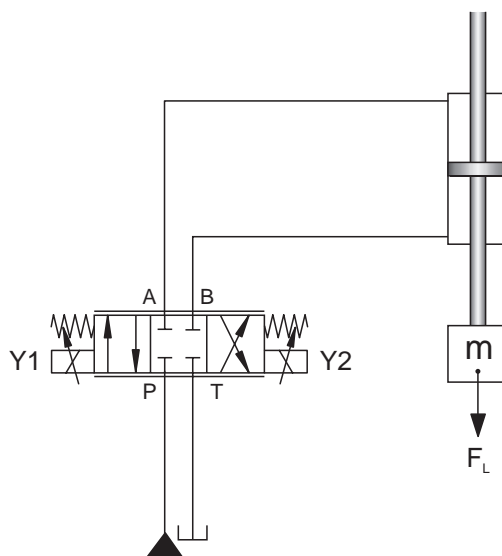


Fig. 6.6
Equal area cylinder drive
with mass load and friction

Example 4 Velocity calculation for an equal area cylinder taking into account frictional and load force

A cylinder drive is mounted vertically and has to lift and lower a load (fig. 6.6).

- The load force is $F_L = 20 \text{ kN}$.
- The frictional force for both motion directions is $F_R = 5 \text{ kN}$.

The remainder of the technical data corresponds to *example 2*.

Required

- the maximum velocity for the upward movement of the drive (correcting variable: $y = 10 \text{ V}$)
- the maximum velocity for the downward movement of the drive (correcting variable: $y = -10 \text{ V}$)
- the required volumetric flow rate of the pump q_P

■ **Maximum velocity without load**

(from *example 2*):

$$v = \frac{q_A}{A_R} = \frac{100 \text{ dm}^3}{60 \text{ s} \cdot 0.393 \text{ dm}^2} = 4.24 \frac{\text{dm}}{\text{s}} = 0.424 \frac{\text{m}}{\text{s}}$$

Calculation of maximum piston force

$$\begin{aligned} F_{\max} &= A_R \cdot p_0 = 39.3 \text{ cm}^2 \cdot 250 \text{ bar} = 39.3 \text{ cm}^2 \cdot 250 \frac{\text{kp}}{\text{cm}^2} \\ &= 9825 \text{ kp} = 98.25 \text{ kN} \end{aligned}$$

■ **Calculation of maximum velocity**

(upward movement, pushing load)

actual piston force

$$F = F_R + F_L = 5 \text{ kN} + 20 \text{ kN} = 25 \text{ kN}$$

Velocity with maximum valve opening

$$v_L = v \cdot \sqrt{\frac{F_{\max} - F}{F_{\max}}} = 0.424 \frac{\text{m}}{\text{s}} \cdot \sqrt{\frac{98.25 \text{ kN} - 25 \text{ kN}}{98.25 \text{ kN}}} = 0.366 \frac{\text{m}}{\text{s}}$$

- **Calculation of maximum velocity**
(downward movement, pulling load)

Actual piston force

$$F = F_R + F_L = 5 \text{ kN} - 20 \text{ kN} = -15 \text{ kN}$$

Speed with maximum valve opening

$$v_L = v \cdot \sqrt{\frac{F_{\max} - F}{F_{\max}}} = 0.424 \frac{\text{m}}{\text{s}} \cdot \sqrt{\frac{98.25 \text{ kN} + 15 \text{ kN}}{98.25 \text{ kN}}} = 0.455 \frac{\text{m}}{\text{s}}$$

- **Calculation of the required volumetric flow rate of the pump**

With a downward movement the velocity v and the volumetric flow rate q_A via the inlet control edge are greater than that with the upward movement. The pump must therefore be sized for the downward movement.

$$q_P = q_{A\max} = v_{\max} \cdot A_R = 4.55 \frac{\text{dm}}{\text{s}} \cdot 0.393 \text{ dm}^2 = 1.79 \frac{\text{dm}^3}{\text{s}} = 107.5 \frac{\text{l}}{\text{min}}$$

Effect of the load force on the motion velocity

The example illustrates the effect of the load force on the motion velocity of a hydraulic cylinder drive:

- With an upward movement the drive has to surmount a force, which acts against the motion direction. The velocity is less with identical valve opening than in the unloaded case.
- With the downward movement, the load acts in the motion direction. The velocity is higher with identical valve opening than in the unloaded case.

6.5 Velocity calculation for an unequal area cylinder taking into account frictional and load forces

Maximum force on the drive piston

The maximum piston force F_{\max} is calculated according to *table 6.7*. The force for the advance sequence is greater by factor α than for the return sequence.

Piston force at constant motion velocity

The same correlations apply as those for the equal area cylinder drive (section 6.4).

Load pressure, chamber pressures and differential pressures across the control edges

The calculation formulae for the load pressure p_L for the return and advance sequence are different (*table 6.7*). An identical load during the return sequence causes a higher load pressure p_L by factor α .

The chamber pressures p_A and p_B as well as the differential pressures Δp_A and Δp_B across the control edges are shown in *fig. 6.7a* (advance sequence) and in *fig. 6.7b* (return sequence).

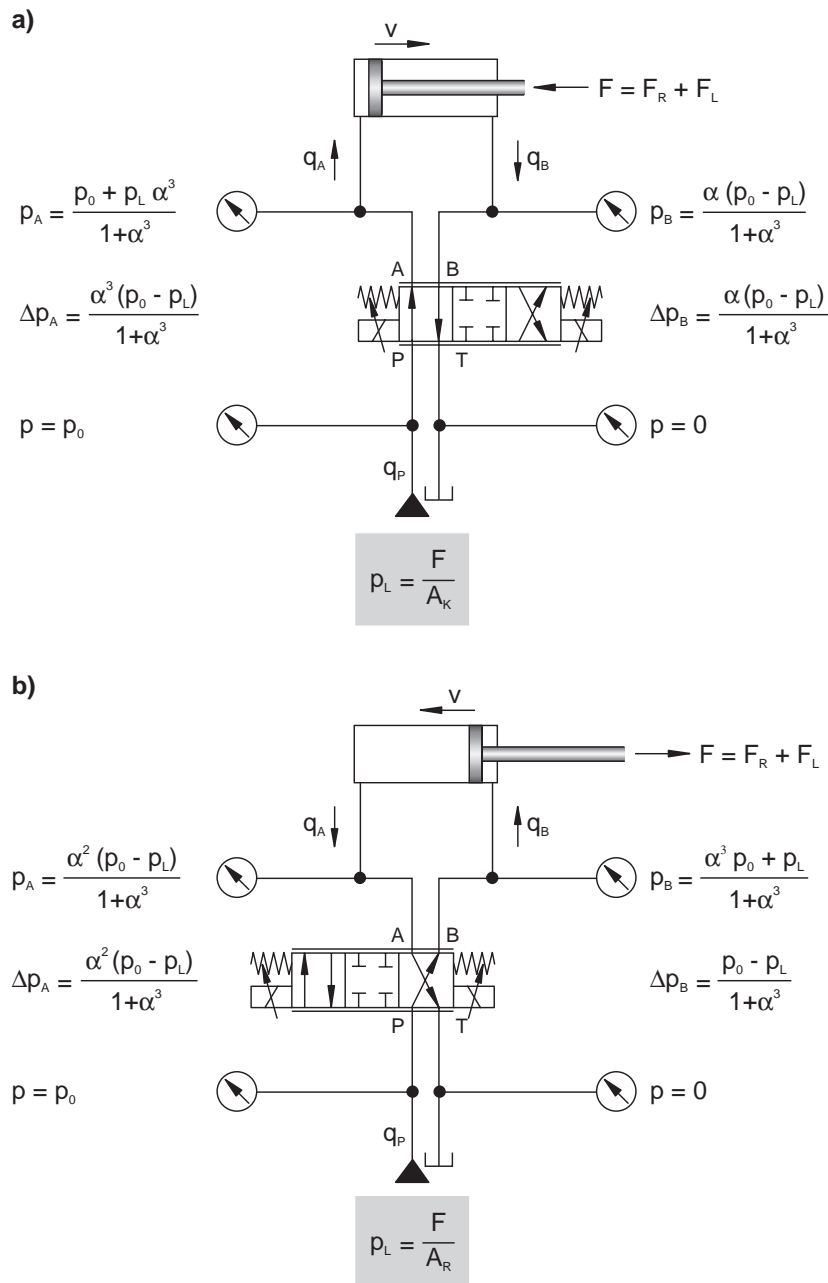


Fig. 6.7
Chamber pressures and differential pressures across control edges with an unequal area cylinder drive (with load and frictional force)

Calculation of return and advance velocity

The return and advance velocity are calculated in accordance with the same principle as that for the equal area cylinder (section 6.4).

Effect of load forces

During the return sequence, the maximum piston force F_{\max} is less than during the advance sequence. A load force acting against the motion direction, leads to a higher load pressure p_L , whereby the velocity influenced by the pushing load is reduced during the return sequence.

Sizing of the pump

The decisive factor for pump sizing is the maximum volumetric flow rate q_{\max} via the inlet control edge, which occurs during valve opening. In order to determine the required volumetric flow rate of the pump, both motion directions need to be examined:

- In the case of most drive systems, the maximum volumetric flow rate via the inlet control edge is greater during advancing. The pump is therefore sized for the advance sequence.
- If a pushing load acts during advancing as opposed to a pulling load during returning, the volumetric flow rate via the inlet control edge may be greater during returning than during advancing. In this case, the pump is to be sized for the return sequence.

a) Parameters of hydraulic drive system	
	see table 6.3
b) Load parameters	
	see table 6.5
c) Advancing of piston rod	
Calculation formulae for cylinder	
Maximum piston force	$F_{\max} = A_K \cdot p_0$
Actual piston force	$F = F_R + F_L$
Load pressure	$p_L = \frac{F}{A_K}$
Calculation of advance velocity	
Flow rate via inlet control edge	$q_A = q_N \cdot \frac{y}{y_{\max}} \cdot \sqrt{\frac{p_0 - p_L}{p_N} \cdot \frac{\alpha^3}{1 + \alpha^3}}$
Velocity with load	$v_L = \frac{q_A}{A_K}$
Calculation of advance velocity, if advance velocity without load known	
Advance velocity without load	v see table 6.3
Advance velocity with load	$v_L = v \cdot \sqrt{\frac{p_0 - p_L}{p_0}} = v \cdot \sqrt{\frac{F_{\max} - F}{F_{\max}}}$
d) Returning of piston rod	
Calculation formulae for cylinder	
Maximum piston force	$F_{\max} = A_R \cdot p_0$
Actual piston force	$F = F_R + F_L$
Load pressure	$p_L = \frac{F}{A_R} = \frac{F \cdot \alpha}{A_K}$
Calculation of return velocity	
Flow rate via inlet control edge	$q_B = q_N \cdot \frac{y}{y_{\max}} \cdot \sqrt{\frac{p_0 - p_L}{p_N} \cdot \frac{1}{1 + \alpha^3}}$
Velocity with load	$v_L = \frac{q_B}{A_R} = \frac{q_B \cdot \alpha}{A_K}$

Table 6.7
Velocity calculation for an unequal area cylinder drive (with load and frictional force)

*Continuation of table 6.7
Velocity calculation for an
unequal area cylinder drive
(with load and frictional
force)*

Calculation of return velocity, if return velocity without load known	
Return velocity without load	v see table 6.3
Return velocity with load	$v_L = v \cdot \sqrt{\frac{p_0 - p_L}{p_0}} = v \cdot \sqrt{\frac{F_{\max} - F}{F_{\max}}}$
e) Calculation formulae for volumetric flow rate of pump	
	$q_P = q_{\max}$

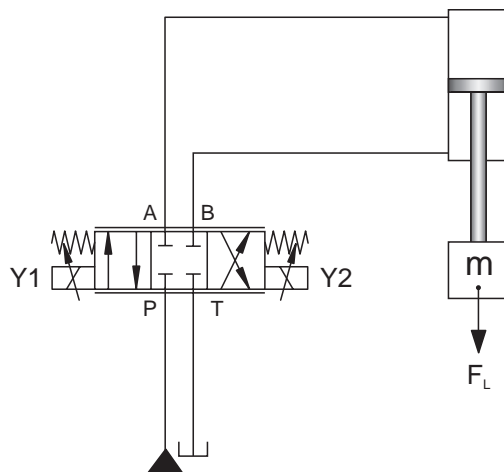


Fig. 6.8
Unequal area cylinder
drive with mass load and
frictional force

Velocity calculation for an unequal area cylinder taking into account frictional and load force

Example 5

An unequal area cylinder drive has been mounted vertically and is to lift and lower a load (*fig. 6.8*). All other data correspond to that for the drive system in *example 4*.

Required

- the maximum velocity for the upward movement of the drive (correcting variable $y = 10 \text{ V}$)
- the maximum velocity for the downward movement of the drive (correcting variable $y = -10 \text{ V}$)
- the required volumetric flow rate of the pump

■ Calculation of maximum velocity for the upwards movement:

The piston rod returns during the upward movement.

Maximum velocity of the return movement without load
(from example 3)

$$v = \frac{q_B}{A_R} = \frac{47.1 \text{ dm}^3}{60 \text{ s} \cdot 0.393 \text{ dm}^2} = 0.2 \frac{\text{m}}{\text{s}}$$

maximum piston force (return movement)

$$F_{\max} = A_R \cdot p_0 = 0.393 \text{ dm}^2 \cdot 250 \text{ bar} = 98.25 \text{ kN}$$

actual piston force

$$F = F_R + F_L = 5 \text{ kN} + 20 \text{ kN} = 25 \text{ kN}$$

Speed for maximum valve opening (return movement)

$$v_L = v \cdot \sqrt{\frac{F_{\max} - F}{F_{\max}}} = 0.2 \frac{\text{m}}{\text{s}} \cdot \sqrt{\frac{98.25 \text{ kN} - 25 \text{ kN}}{98.25 \text{ kN}}} = 0.173 \frac{\text{m}}{\text{s}}$$

■ Calculation of maximum velocity for the downward movement:

The piston rod advances during the downward movement.

Maximum velocity of the advance movement without load
(from example 3)

$$v = \frac{q_A}{A_K} = \frac{133.3 \text{ dm}^3}{60 \text{ s} \cdot 0.785 \text{ dm}^2} = 0.28 \frac{\text{m}}{\text{s}}$$

maximum piston force (advance movement)

$$F_{\max} = A_K \cdot p_0 = 0.785 \text{ dm}^2 \cdot 250 \text{ bar} = 196.3 \text{ kN}$$

actual piston force

$$F = F_R - F_L = 5 \text{ kN} - 20 \text{ kN} = -15 \text{ kN}$$

Velocity during maximum valve opening (advance movement)

$$v_L = v \cdot \sqrt{\frac{F_{\max} - F}{F_{\max}}} = 0.28 \frac{\text{m}}{\text{s}} \cdot \sqrt{\frac{196.3 \text{ kN} + 15 \text{ kN}}{196.3 \text{ kN}}} = 0.29 \frac{\text{m}}{\text{s}}$$

■ **Calculation of the required volumetric flow rate of the pump:**

maximum volumetric flow rate via the inlet control edge during advancing

$$q_A = v_L \cdot A_K = 0.29 \frac{\text{m}}{\text{s}} \cdot 0.785 \text{ dm}^2 = 2.3 \frac{\text{dm}^3}{\text{s}} = 137 \frac{\text{l}}{\text{min}}$$

maximum volumetric flow rate via the inlet control edge during returning

$$q_B = v_L \cdot A_R = 0.173 \frac{\text{m}}{\text{s}} \cdot 0.393 \text{ dm}^2 = 0.68 \frac{\text{dm}^3}{\text{s}} = 40.8 \frac{\text{l}}{\text{min}}$$

required volumetric flow rate of the pump

$$q_P = q_{\max} = q_A = 137 \frac{\text{l}}{\text{min}}$$

Velocity and control variable pattern during the acceleration phase

To make a rough calculation, a constant acceleration rate is assumed. This produces a constant, increasing velocity during the acceleration phase (*fig. 6.2*). The valve opening is increased in ramp form during the acceleration phase.

Forces during the acceleration phase

During the acceleration phase, the piston force F is made up of the frictional force F_R , load force F_L and acceleration force F_B . The maximum acceleration force and the maximum acceleration a_{\max} occur with maximum piston force F_{\max} . The maximum piston force F_{\max} is achieved, if the supply pressure p_0 , prevails in one cylinder chamber and the tank pressure in the other chamber.

The formulae for the force during acceleration are summarised in *table 6.8a*.

6.6 Effect of the maximum piston force on the acceleration and delay process

Duration of acceleration process and distance travelled

In order to achieve a fast motion sequence, the acceleration needs to be as great as possible. The maximum achievable acceleration a_{\max} is calculated as a quotient of the maximum acceleration force $F_{B\max}$ and moving mass m (*table 6.8b*). The total moved mass m is determined by adding the load mass and the mass of the hydraulic drive.

The duration of the acceleration process t_B and the distance travelled x_B is calculated according to *table 6.8b*.

Velocity variable and correcting variable pattern of the delay phase

Since the prerequisite for the delay phase is a constant delay, this results in a constant, reducing velocity (*fig. 6.2*). The valve opening is reduced in ramp form until the valve is closed.

Effective direction of forces during delaying

During the delay process, the resulting force F exerted by the piston on the load is in the opposite direction to the motion direction. It therefore becomes positive, if it acts against the motion direction. The frictional force F_R and a positive load force F_L support the delay process (*table 6.8c*) and reduce the piston force F required for delay.

Cavitation and pressure surge

In order to decelerate (= delay) a cylinder drive, the proportional directional control valve needs to be closed. Two effects occur, if the valve opening is reduced to quickly:

- In the chamber, in which the pressure fluid is compressed by the moving load, the pressure increases suddenly above the supply pressure. The cylinders, connectors and pipes may burst as a result of the pressure surge.
- In the other chambers, the pressure drop below the tank pressure and cavitation occurs.

Critical piston force values during delaying

In order to prevent cavitation and an excessive pressure surge during the deceleration of an equal area cylinder, the valve must be closed slowly enough in order for the piston force F to remain under a critical value F_{\max} . The permissible piston forces during delaying are listed in *table 6.8c*.

- With an equal area cylinder drive, the maximum force F_{\max} calculated for acceleration must not be exceeded.
- If the returning piston rod of an unequal area cylinder is decelerated, then the risk of cavitation is minimal, since comparatively little oil flows through the inlet control edge. It is advisable to decelerate the drive in such a way that the pressure on the piston area does not rise above the supply pressure. The maximum piston force is calculated under these conditions according to *table 6.8c*.
- Particularly critical is the braking of an advancing unequal area drive, since in this case cavitation readily occurs with a comparatively reduced piston force F_{\max} .

Duration of the delay process and distanced travelled

The drive reaches the maximum delay a_{\max} , when the maximum piston force F_{\max} acts against the motion direction (*table 6.8c*).

The maximum delay a_{\max} , the duration t_V of the delay process and the distance travelled x_V are calculated according to *table 6.8d*.

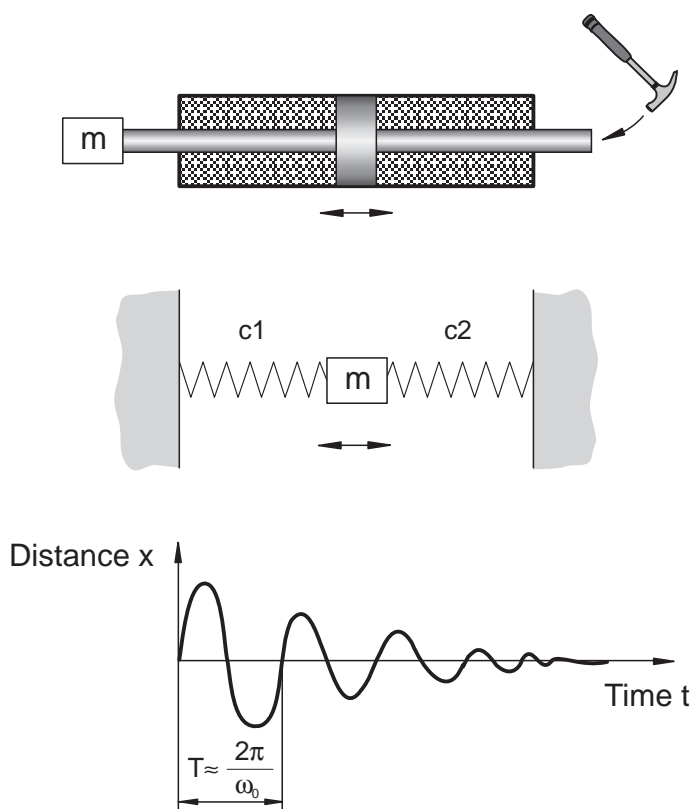
a) Calculation formulae for the forces during the acceleration phase	
Piston force during the acceleration phase	$F = F_B + F_R + F_L$
Maximum piston force of equal area cylinder	$F_{\max} = A_R \cdot p_0$
Maximum piston force of unequal area cylinder during advancing	$F_{\max} = A_K \cdot p_0$
Maximum piston force of unequal area cylinder during returning	$F_{\max} = A_R \cdot p_0$
b) Calculation formulae for duration of the acceleration phase and the distance travelled	
Permissible maximum acceleration	$a_{\max} = \frac{F_{B\max}}{m} = \frac{F_{\max} - F_R - F_L}{m}$
Duration of acceleration phase	$t_B = \frac{v}{a}$
Distance travelled during the acceleration phase	$x_B = \frac{1}{2} \cdot t_B \cdot v$
c) Calculation formulae for forces during delay phase	
Piston force during delay phase	$F = F_V - F_R - F_L$
Maximum piston force of equal area cylinder	$F_{\max} = A_R \cdot p_0$
Maximum piston force of unequal area cylinder during advancing	$F_{\max} = \frac{A_K \cdot p_0}{\alpha^3}$
Maximum piston force of unequal area cylinder during returning	$F_{\max} = A_K \cdot p_0 \cdot \frac{\alpha^3 - \alpha^2 + 1}{\alpha^3}$
d) Calculation formulae for duration of delay phase and distance travelled	
Permissible maximum delay	$a_{\max} = \frac{F_{V\max}}{m} = \frac{F_{\max} + F_R + F_L}{m}$
Duration of delay phase	$t_V = \frac{v}{a}$
Distance travelled during delay phase	$x_V = \frac{1}{2} \cdot t_V \cdot v$

Table 6.8
Effect of maximum piston force on the acceleration and delay process

Hydraulic cylinder drive as spring/mass oscillator

The piston of a double-acting hydraulic cylinder is clamped between two liquid columns. Since the fluid is compressible, the columns form springs with spring stiffnesses c_1 and c_2 (fig. 6.9). The spring stiffnesses of the two columns are cumulative. With an equal area cylinder drive, the sum of the two spring stiffnesses is lowest when the piston is in mid-position.

The system consisting of oil springs, piston, piston rod and mass load may be regarded as a spring/mass oscillator. If a hydraulic cylinder drive with closed valve is excited by a force, diminishing oscillations occur (fig. 6.9).



6.7 Effect of natural angular frequency on the acceleration and delay process

Fig. 6.9
Hydraulic cylinder
drive as spring/mass
oscillator

Calculation of natural angular frequency

The spring stiffness c of an equal area hydraulic cylinder drive in mid-position is calculated from the compression modulus E of the hydraulic fluid as well as the stroke H and the annular area A_R (table 6.7). Inclusion of the moving mass m in the formula of the spring/mass oscillators leads to the natural angular frequency ω_0 of the hydraulic drive.

With a drive system, it is not just the fluid volume which is compressed into the cylinder chamber, but in addition the fluid volumes in the pipes between the valve and the drive. As a result of the effect of the pipes, the compressed fluid volume rises and the spring stiffness c drops. With this natural angular frequency ω_0 is also reduced. This can be taken into account when calculating the natural angular frequency by means of an overall correction factor of 0.85 to 0.9.

With an unequal area cylinder drive, the minimum of the natural angular frequency is outside the piston mid-position. The calculation formula for the minimum natural angular frequency is listed in table 6.9 and includes the correction factor.

Calculation of minimum acceleration and delay time

In order to prevent oscillations, the acceleration time t_B and the delay time t_V of a hydraulic cylinder drive selected must not be too short. The permissible minimum acceleration and delay times depend on the natural angular frequency. The higher the natural angular frequency, the faster the acceleration and delay of the drive permitted (table 6.9). Distances x_B and x_V travelled by the drive during the two phases, can be calculated from the acceleration and delay time.

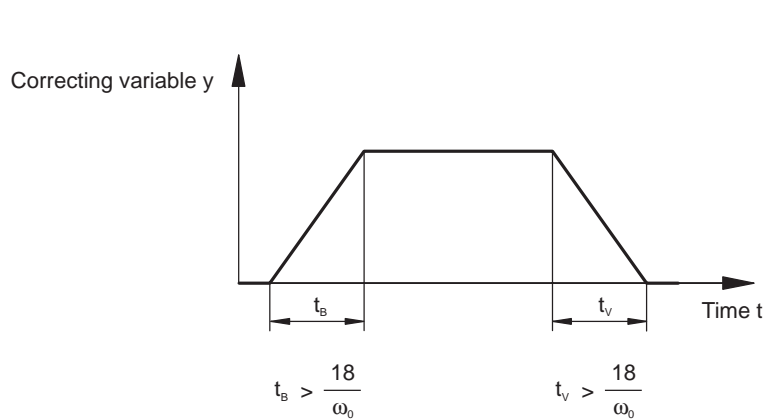


Fig. 6.10
Minimum ramp time,
governed by natural
angular frequency

Parameters of hydraulic drive system	
	see table 6.3
Compression modulus of pressure fluid	E
Cylinder stroke	H
Calculation formulae for natural angular frequency of equal area cylinder drive	
Minimum spring stiffness of the two fluid columns	$c = c_1 + c_2 = \frac{2 \cdot E \cdot A_R}{H} + \frac{2 \cdot E \cdot A_R}{H} = \frac{4 \cdot E \cdot A_R}{H}$
Minimum natural angular frequency	$\omega_0 = \sqrt{\frac{c}{m}} = \sqrt{\frac{4 \cdot E \cdot A_R}{H \cdot m}}$
Minimum natural angular frequency with dead volume	$\omega_0 \approx 0.85 \dots 0.9 \sqrt{\frac{4 \cdot E \cdot A_R}{H \cdot m}}$
Calculation formulae for natural angular frequency of unequal area cylinder drive	
Minimum natural angular frequency with dead volume	$\omega_0 = 0.85 \dots 0.9 \cdot \sqrt{\frac{4 \cdot E \cdot A_K}{H \cdot m}} \cdot \frac{1 + \sqrt{\alpha}}{2 \cdot \sqrt{\alpha}}$
Calculation formulae for motion sequence	
Minimum acceleration and delay time	$t_{Bmin} = t_{Vmin} = \frac{18}{\omega_0}$
Minimum acceleration and delay distance	$x_{Bmin} = x_{Vmin} = \frac{1}{2} \cdot v \cdot t_{Bmin} = \frac{1}{2} \cdot v \cdot t_{Vmin} = \frac{9 \cdot v}{\omega_0}$

*Table 6.9
Calculation of natural angular frequency and its effect on the acceleration and delay phase*

Example 6 Calculation of natural angular frequency and minimum permissible acceleration and delay time for an unequal area cylinder

An unequal area hydraulic cylinder drive is to lift and lower a mass. The data corresponds to the drive system in *example 6 (fig. 6.8)*. The stroke H of the cylinder is 1m, the compression modulus E is $1.4 \cdot 10^9 \text{ N/m}^2$.

Required

- Minimum natural angular frequency of the drive system
- Minimum permissible acceleration and delay time

■ **Calculation of minimum natural angular frequency**

Minimum natural angular frequency

$$\begin{aligned}\omega_0 &= 0.9 \cdot \sqrt{\frac{4 \cdot E \cdot A_K}{H \cdot m} \cdot \frac{1 + \sqrt{\alpha}}{2 \cdot \sqrt{\alpha}}} \\ &= 0.9 \cdot \sqrt{\frac{4 \cdot 1.4 \cdot 10^9 \cdot \frac{\text{N}}{\text{m}^2} \cdot 7.85 \cdot 10^{-3} \cdot \text{m}^2}{1 \text{m} \cdot 2000 \text{ kg}}} \cdot \frac{1 + \sqrt{2}}{2 \cdot \sqrt{2}} = 113.9 \cdot \frac{1}{\text{s}}\end{aligned}$$

■ **Calculation of the minimum acceleration and delay time**

Minimum acceleration and delay time

$$t_{B\min} = t_{V\min} = \frac{18}{\omega_0} = 0.158 \text{ s}$$

Calculation steps

The duration of the motion sequence is calculated via the following steps:

- Establishing the maximum velocity,
- Calculation of duration of the acceleration and delay phase,
- Decision as to whether the motion sequence consists of two or three phases,
- Calculation of overall duration of motion.

Calculation of maximum velocity

The maximum velocity depends on the maximum valve opening, the piston or annular area, the supply pressure and the load. The calculation formulae are given and explained in section 6.4 and 6.5.

Duration of the acceleration and delay phase

During the acceleration and delay phase, the valve is opened or closed in ramp form.

The permissible acceleration and delay is determined by two influencing variables:

- The permissible piston forces calculated in section 6.6 must not be exceeded.
- The ramps during acceleration and deceleration must be selected in such a way that the drive is not excited into oscillations (section 6.7).

The duration of the acceleration phase t_B and the duration of the delay phase t_V are determined in such a way as to fulfil both conditions. This is followed by the calculated distances x_B and x_V , which have been covered during the acceleration and delay phase.

6.8 Calculation of motion duration

Motion sequence with three phases

If the sum of the two distances x_B and x_V is less than the overall distance, the motion sequence has three phases (*fig. 6.2*). The drive completes the remaining distance x_K at maximum velocity. The entire motion sequence requires a time duration t_G , which is calculated by adding together t_B , t_K and t_V .

Motion sequence with two phases

If the sum of the calculated distances x_B and x_V equals the overall distance x_G , the motion sequence consists of two phases and the calculation is complete.

If the sum of the two calculated distances x_B and x_V is greater than the overall distance x_G , the maximum velocity possible on the drive side will not be reached during the motion. In this case, the motion sequences comprise two phases and the distances x_B and x_V must be determined afresh. To do this, the maximum permissible piston forces and the limits specified by the natural angular frequency must be taken into account. The duration of the acceleration and delay process is then calculated from the distances x_B and x_V and by adding the entire motion duration t_G .

Example 7 Calculation of duration of a motion sequence with unequal area cylinders.

An unequal area cylinder drive is to lift and lower a mass. The technical data corresponds to that in *example 6*.

Required

the minimum overall duration t_G of the motion, if the load is lower by $x_G = 0.5$ m.

■ **Establishing the motion type**

The motion in question is an advance movement of an unequal area cylinder.

- **Calculation of maximum speed for downward movement according to *example 5*.**

$$v_L = v \cdot \sqrt{\frac{F_{\max} - F}{F_{\max}}} = 0.29 \frac{\text{m}}{\text{s}}$$

- **Acceleration phase**

maximum piston force

$$F_{\max} = A_K \cdot p_0 = 0.785 \text{ dm}^2 \cdot 250 \text{ bar} = 196.3 \text{ kN}$$

maximum acceleration force

$$F_B = F_{\max} - F_R - F_L = 196.3 \text{ kN} - 5 \text{ kN} + 20 \text{ kN} = 211.3 \text{ kN}$$

minimum duration of acceleration phase
(restriction through force)

$$t_{B\min1} = \frac{v_L}{a} = \frac{v_L \cdot m}{F_B} = \frac{0.29 \frac{\text{m}}{\text{s}} \cdot 2000 \text{ kg}}{211.3 \text{ kN}} = 2.7 \text{ ms}$$

minimum duration of acceleration phase
(restriction through natural angular frequency, according to *example 6*)

$$t_{B\min2} = \frac{18}{\omega_0} = 158 \text{ ms}$$

minimum duration of acceleration phase

$$t_B = t_{B\max} = t_{B\min2} = 158 \text{ ms}$$

Distance covered during the acceleration phase

$$x_B = \frac{1}{2} \cdot v_L \cdot t_B = \frac{1}{2} \cdot 0.29 \frac{\text{m}}{\text{s}} \cdot 0.158 \text{ s} = 2.3 \text{ cm}$$

■ Delay phase

maximum piston force

$$F_{\max} = \frac{p_0 \cdot A_K}{\alpha^3} = \frac{196.3 \text{ kN}}{8} = 24.5 \text{ kN}$$

maximum delay force

$$F_V = F_{\max} + F_R + F_L = 24.5 \text{ kN} + 5 \text{ kN} - 20 \text{ kN} = 9.5 \text{ kN}$$

minimum duration of delay phase
(restriction through force)

$$t_{V\min1} = \frac{v_L}{a} = \frac{v_L \cdot m}{F_V} = \frac{0.29 \frac{\text{m}}{\text{s}} \cdot 2000 \text{ kg}}{9.5 \text{ kN}} = 61 \text{ ms}$$

minimum duration of delay phase
(restriction through natural angular frequency)

$$t_{V\min2} = \frac{18}{\omega_0} = 158 \text{ ms}$$

minimum duration of delay phase

$$t_V = t_{V\max} = t_{V\min2} = 158 \text{ ms}$$

Distance covered during the delay phase

$$x_V = \frac{1}{2} \cdot v_L \cdot t_V = \frac{1}{2} \cdot 0.29 \frac{\text{m}}{\text{s}} \cdot 0.158 \text{ s} = 2.3 \text{ cm}$$

■ Conclusion

The distance covered during the acceleration and delay phase is smaller overall than the overall distance x_G . Conclusion: The motion sequence consists of three phases.

■ Maximum velocity phase

Distance with constant travel

$$x_K = x_G - x_B - x_V = 0.5 \text{ m} - 0.23 \text{ m} - 0.23 \text{ m} = 0.454 \text{ m}$$

Duration of constant travel

$$t_K = \frac{x_K}{v_L} = \frac{0.454 \text{ m}}{0.29 \frac{\text{m}}{\text{s}}} = 1.56 \text{ s}$$

■ Overall duration of motion

$$t_G = t_B + t_V + t_K = 0.158 \text{ s} + 0.158 \text{ s} + 1.56 \text{ s} = 1.87 \text{ s}$$

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Chapter 6